

# STUDY ON HEAT TRANSFER CHARACTERISTICS OF A VOLUMETRIC SOLAR RECEIVERS

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## ABSTRACT

In this paper, study on a volumetric receiver which use for solar energy season storage and heating system. This type of volumetric receiver has a high heat capacity, so that volumetric receiver can be ensured under severe weather conditions. In order to provide a reference for design and modification of volumetric receiver, the heat

transfer characteristics of the volumetric heat absorber are studied. The influence of extinction coefficient and wind speed on the heat transfer characteristics of the volumetric receiver is analyzed by single factor analysis.

**Keywords:** volumetric receiver, high heat capacity, heat transfer characteristics

<i>Symbols</i>	<i>Interpretation</i>
$A$	Area ( $m^2$ )
$c$	specific heat ( $J/(kg \cdot ^\circ C)$ )
$d_{ab}$	equivalent particle diameter (m)
$d_p$	average pore diameter (m)
$r$	thickness( m )
$v$	velocity( m/s)
$L_1$	receiver height ( m )
$L_2$	receiver width ( m )
$L_3$	receiver length ( m )
$I$	thermal flux ( $W/m^2$ )
<i>Greek characters</i>	
$\alpha$	absorption rate
$\alpha_{sf}$	surface area density( $m^{-1}$ )
$\beta$	extinction coefficient
$\gamma$	reflectivity
$\rho$	density( $kg/m^3$ )
$\lambda$	thermal conductivity( $W/(m \cdot ^\circ C)$ )
$t$	temperature ( $^\circ C$ )
$\varepsilon$	porosity
$h$	heat transfer coefficient( $W/(m^2 \cdot ^\circ C)$ )
$h_v$	volumetric heat transfer coefficient ( $W/(m^3 \cdot ^\circ C)$ )

## *Dimensionless*

### *numbers*

$Nu$	Nusselt number
$Ra$	Rayleigh number
$Pr$	Prandtl number
$Re$	Reynolds number
$Gr$	Grashof number

### *Subscripts*

$g$	glass window
$a$	air
$ab$	porous ceramic absorber panel
$w$	water

### *Abbreviation*

$s$	
$DNI$	direct normal irradiance( $W/m^2$ )

## 1. INTRODUCTION

In the solar heat storage and heating system by using the season storage body, the temperature stratification of the season storage body is beneficial to improve the system performance of the solar heat storage and heating system[1-2]. In order to improve the temperature stratification of the seasonal storage body in the tower solar energy

season storage and heating system, Zhifeng Wang et al. proposed a volumetric receiver which use in tower solar collector system with a higher heat capacity. This volumetric receiver has a high heat capacity, so it can ensure the outlet temperature of volumetric receiver under complicated weather conditions, and is favorable for temperature stratification of the season storage body.

At present, there are few related researches on such volumetric receiver. Therefore, in order to provide reference for the design and modification on volumetric receiver, a one-dimensional unsteady model of volumetric receiver is established. The model is solved by MATLAB software, and the influence of glass extinction coefficient and wind speed on the heat transfer characteristics of the volumetric receiver was analyzed.

## 2. MODELLING

### 2.1 Physical model

The physical structure of the volumetric receiver studied in this paper is shown in Fig. 1. The volumetric receiver is composed of a glass window, porous ceramic absorber panel, a supporting structure and an insulating layer.

When the volumetric receiver is working, the focused solar radiation is incident on the volumetric receiver, part of the solar radiation is absorbed by the glass window and the absorber panel and converted into heat energy which is then transferred to the water by convection heat transfer. The remaining solar radiation passing through the glass window is directly absorbed by the water as internal energy of the water. The cold water enters the volumetric receiver from the bottom and is heated and discharged from the top of the volumetric heat absorber.

Therefore, when the volumetric receiver is working, the heat transfer process of the volumetric receiver mainly includes the absorption of incident solar radiation by the water, the glass window and the absorber plane. The convective heat transfer of glass window between the air and the water. The convective heat transfer between the absorber

plane and the water. The heat conduction of the glass window and the absorber plane. Since the volumetric receiver is mainly used in a solar heating system and the working temperature is not high, the radiation heat exchange between the glass window, the absorber plane and the water can be neglected. The insulation is very good, so the convective heat loss between the insulation layer and the air can be neglected.

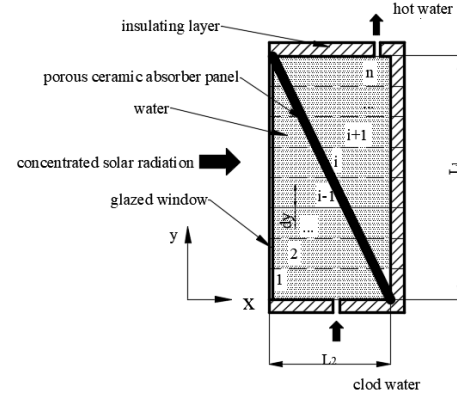


Fig.1 Physical structure of a volumetric receiver

### 2.2 Governing equations

A reduced-order unsteady model of a volumetric receiver was developed by simplifying the three-dimensional volumetric receiver design based on the following assumptions:

(1) The absorption of the solar insolation incident on the volumetric receiver can be described by a one-dimensional normal distribution in the y direction.

(2) The temperatures of the porous ceramic absorber panel, the glass window and the water are uniform in the x direction

(3) The surfaces are all adiabatic.

(4) The water flow inside the receiver can be modeled as plug flow.

With these assumptions, the energy equations for volumetric receiver can be given as:

For the glass window:

$$c_g \rho_g \frac{\partial t_g}{\partial \tau} = \lambda_g \frac{\partial^2 t_g}{\partial y^2} + \frac{h_{g,a}}{r_g} (t_a - t_g) + \frac{h_{g,w}}{r_g} (t_w - t_g) + \frac{I_g}{r_g} (1 - \gamma_g) (1 - e^{-\beta_g r_g}) \quad (1)$$

Where  $\beta_g$  is the extinction coefficient of the glass and  $r_g$  is the thickness of the glass. The  $\gamma_g$  is reflectance of the glass surface.

For the porous ceramic absorber panel:

$$(1-\varepsilon)c_{ab}\rho_{ab}\frac{\partial t_{ab}}{\partial \tau}=(1-\varepsilon)\lambda_{ab}\frac{\partial^2 t_{ab}}{\partial y^2}+h_v(t_w-t_{ab})+\frac{I_{ab}}{r_{ab}}(1-e^{-\beta_g r_g}) \quad (2)$$

For the water:

$$c_w\rho_w\left(\frac{\partial t_w}{\partial \tau}+v_w\frac{\partial t_w}{\partial y}\right)=\lambda_w\frac{\partial^2 t_w}{\partial y^2}+h_v(t_{ab}-t_w)+\frac{h_{g,w}}{r_g}(t_g-t_w)+\frac{I_w}{L_2}\alpha_w \quad (3)$$

In Eq.(1) the  $l_g$  is the solar radiant energy density incident on the glass window can be calculated as[3-4]:

$$I_g=\frac{A_{hel}}{A_g}DNI\frac{1}{\sqrt{2\pi(L_1^*/\delta)}}e^{-\frac{[y-(L_1/2+\mu)]^2}{2(L_1^*/\delta)}} \quad (4)$$

Where  $A_{hel}$  is concentrator field aperture area and  $A_g$  is glass window area. The  $L_1^*$  is dimensionless length and the  $\mu$  is correction factor.

In Eq. (3) the  $l_w$  is the solar radiant energy density incident on the water can be calculated as:

$$I_w=I_g e^{-\beta_g r_g} \quad (5)$$

In Eq. (2) the  $l_{ab}$  is the solar radiant energy density incident on the absorber plane can be calculated as:

$$I_{ab}=I_w(1-\alpha_w) \quad (6)$$

In Eq. (2) the  $\beta_{ab}$  is the extinction coefficient of the porous ceramic absorber panel can be calculated as[5-8]:

$$\beta_{ab}=\frac{0.56}{d_{ab}} \quad (7)$$

Where  $d_{ab}$  is the average pore diameter of the porous ceramic absorber panel.

In Eq. (2) the  $h_v$  is the volumetric heat transfer coefficients of the porous ceramic absorber panel can be calculated by[9-10]:

$$h_v=\alpha_{sf}h_{sf} \quad (8)$$

Where  $\alpha_{sf}$  is the surface area density of the porous ceramic absorber panel.

The volumetric heat transfer coefficient can then be calculated as:

$$\alpha_{sf}=\frac{20.346(1-\varepsilon)\varepsilon^2}{d_p} \quad (9)$$

$$d_p=\frac{4\varepsilon}{\alpha_{sf}} \quad (10)$$

$$h_{sf}=0.0035\left(\frac{d_v}{d_p}\right)^{0.35}\left(\frac{\lambda_f}{d_p}\right)Pr^{0.33}Re_d^{0.7089}, Re_d \leq 75 \quad (11)$$

$$h_{sf}=1.064\left(\frac{\lambda_f}{d_p}\right)Pr^{0.33}Re_d^{0.59}, Re_d \geq 350 \quad (12)$$

Where  $d_p$  is equivalent particle diameter of the porous ceramic absorber panel.

when  $75 < Re_d < 350$ ,  $h_{sf}$  is obtained by linear interpolation of Eqs. (11) and (12). The  $Re_d$  is defined as:

$$Re_d=\frac{v_w d_p}{\nu_w} \quad (13)$$

In Eq.(1) and (3) the  $h$  is the convective heat transfer coefficient can be calculated by:

$$h=Nu\frac{\lambda}{l} \quad (14)$$

Where  $l$  is feature length of the glass window.

Since the glass window converts part of the solar radiation into heat energy, the influence of natural convection on convective heat transfer must be considered when calculating the convective heat transfer coefficient of the glass surface.

The reference [11-12] gives the basis for the judgment of mixed convection under the condition that both natural convection and forced convection exist simultaneously.

When  $Gr_w/Re_w^2 < 0.1$ , the effect of natural convection can be ignored. When  $0.1 \leq Gr_w/Re_w^2 \leq 10$ , the flow is in the mixed convection regime. When  $Gr_w/Re_w^2 > 10$ , the effect of forced convection can be neglected.

In the mixed convection condition, if forced convection is in the same direction as natural

convection, the Nusselt number can be calculated as:

$$Nu = \sqrt[3]{Nu_n^3 + Nu_p^3} \quad (15)$$

Where the  $Nu_n$  is the natural convection heat transfer coefficient can be calculated by[13]:

$$Nu_n = 0.825 + \frac{0.387Ra_l^{1/6}}{[1 + (0.492 / Pr)^{9/16}]^{8/27}} \quad (16)$$

And the  $Nu_p$  is the forced convection heat transfer coefficient can be calculated by:

$$Nu_p = 0.664Re_l^{1/2} Pr^{1/3}, (Re \leq 5 \times 10^5, Pr \geq 0.6) \quad (17)$$

Boundary conditions and initial conditions are

$$\begin{cases} \frac{\partial t_g}{\partial x} = \frac{\partial t_w}{\partial x} = \frac{\partial t_{ab}}{\partial x} = 0, & x = 0 \\ t_w = t_{w,in}, & x = 0 \\ \frac{\partial t_g}{\partial x} = \frac{\partial t_w}{\partial x} = \frac{\partial t_{ab}}{\partial x} = 0, & x = L_1 \\ t_g = t_w = t_{ab}, \quad \tau = 0 \end{cases} \quad (18)$$

### 2.3 Solution method and calculation parameters

In order to solve the receiver model, the volumetric receiver is first uniformly cut into several regions along the y direction, as shown in Figure 1. Using the control volume balance method [14], the corresponding equations in the model are integrated on each region of the volumetric receiver to discretize the energy balance equation. The calculation program is written by MATLAB software to solve the discrete energy balance equation.

In order to avoid the influence of other parameters other than the analysis object on the analysis results, in the following analysis process, the parameters involved in the model are unified, as shown in Table 1.

Table 1 parameters used in model

Item	Number
Wind speed (m/s)	6
inlet temperature (°C)	10
DNI (W <sup>2</sup> /m)	600
air temperature (°C)	20
extinction coefficient of glass (m <sup>-1</sup> )	10

concentrator field aperture area(m <sup>2</sup> )	738
flow rate (m <sup>3</sup> /h)	6
receiver height L <sub>1</sub> (m)	1.9
receiver width L <sub>2</sub> (m)	0.738
receiver length L <sub>3</sub> (m)	2.88
thickness of glass r <sub>g</sub> (m)	0.01
thickness of absorber panel r <sub>ab</sub> (m)	0.02

## 3. RESULTS AND DISCUSSION

### 3.1 The thermal efficiency of the volumetric receiver

In order to study the thermal performance of the volumetric receiver, the thermal efficiency of the volumetric receiver is defined here to evaluate the thermal performance of the volumetric receiver. When the volumetric receiver is in steady state, the thermal efficiency of the volumetric receiver can be calculated as:

$$\eta_{rec} = \frac{\int_{\tau_1}^{\tau_2} c_w m_w (t_{w,out} - t_{w,in}) d\tau}{\int_{\tau_1}^{\tau_2} \left( \int_0^{L_1} I_g dy \right) d\tau} \quad (19)$$

### 3.2 The Effect of glass extinction coefficient

The Fig.2 shows the temperature distribution of the glass window under six different glass extinction coefficients when the other parameters are the same.

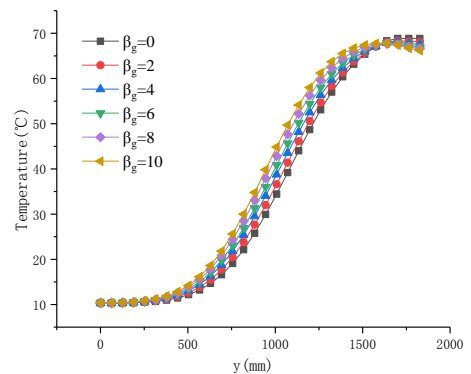


Fig.2 temperature distribution of the glass window

As shown in Fig 2, when the extinction coefficient of the glass is 0 m<sup>-1</sup>, the average temperature of the glass window is 37.5°C, and the maximum temperature of the glass window is 68.9

°C. As the glass extinction coefficient increases, the average temperature of the glass window also increases, but the maximum temperature has dropped. When the extinction coefficient of the glass is increased to  $10 \text{ m}^{-1}$ , the average temperature of the glass window is  $41.6 \text{ }^\circ\text{C}$ , which is increased by  $4.1 \text{ }^\circ\text{C}$ ; the maximum temperature of the glass window is  $67.8 \text{ }^\circ\text{C}$ . It dropped by  $1.1 \text{ }^\circ\text{C}$ .

The Fig.3 shows the temperature distribution of the water under different glass extinction coefficients when the other parameters are the same. It can be seen from Fig.3 that as the glass extinction coefficient increases, the average temperature and the maximum temperature of the water will decrease. When the extinction coefficient of the glass is  $0 \text{ m}^{-1}$ , The average temperature of the water is  $34.9 \text{ }^\circ\text{C}$ , the maximum temperature of the water is  $69.2 \text{ }^\circ\text{C}$ ; when the extinction coefficient of the glass is increased to  $10 \text{ m}^{-1}$ , the average temperature of water is  $33.4 \text{ }^\circ\text{C}$ , which was reduced by  $1.5 \text{ }^\circ\text{C}$ ; the maximum temperature of the water is  $65.5 \text{ }^\circ\text{C}$ , which dropped by  $3.7 \text{ }^\circ\text{C}$ .

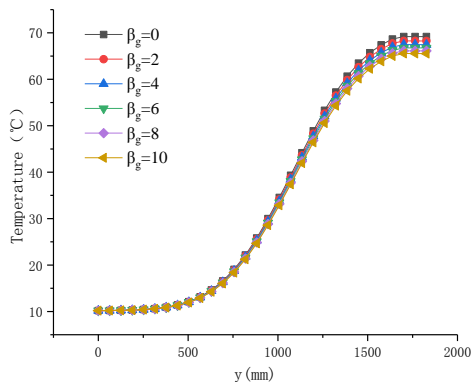


Fig.3 temperature distribution of the glass window

The Fig.4 shows the effect of the extinction coefficient of glass on the convective heat transfer coefficient of the glazing surface.

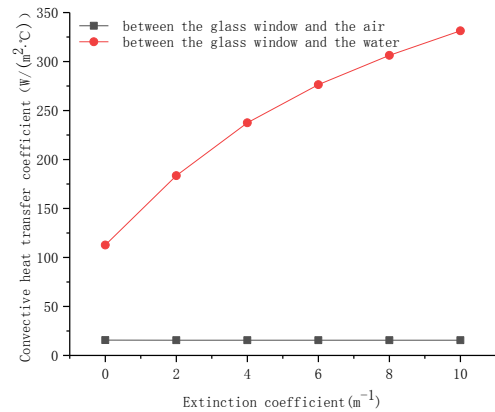


Fig.4 The effect of the extinction coefficient of glass on the convective heat transfer coefficient

It can be seen from Fig.4 that as the extinction coefficient of glass increases, the convective heat transfer coefficient between the water and the glass window increases, but the convective heat transfer between the glass window and the air is almost unchanged. When the extinction coefficient of glass is  $0 \text{ m}^{-1}$ , the convective heat transfer coefficient between the water and the glass window is  $112 \text{ W}/(\text{m}^2 \cdot ^\circ\text{C})$ , when the extinction coefficient of glass is increased to  $10 \text{ m}^{-1}$ , the convective heat transfer coefficient between the water and the glass window rises to  $331 \text{ W}/(\text{m}^2 \cdot ^\circ\text{C})$ .

As shown in Fig.5, the efficiency of the volumetric receiver decreases with the increase of the extinction coefficient of glass. When the extinction coefficient of the glass is  $0 \text{ m}^{-1}$ , the thermal efficiency of the volume receiver is  $92.2\%$ ; When the extinction coefficient of the glass increase to  $10 \text{ m}^{-1}$ , the thermal efficiency of the volumetric receiver is  $86.1\%$ , decrease of  $6.1$  percentage points.

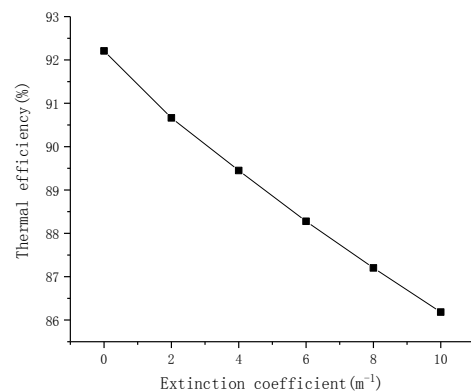


Fig.5 Effect of extinction coefficient on thermal efficiency

### 3.3 The Effect of glass extinction coefficient

The Fig.6 shows the temperature distribution of the glass window under different wind speeds when the other parameters are the same.

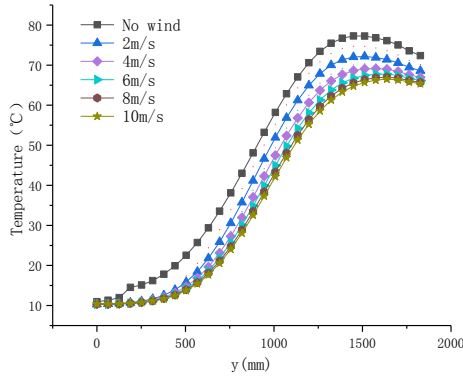


Fig.6 Effect of wind speed on temperature distribution of the glass window

It can be seen from Fig.6 that as the wind speed increases, the average temperature and the maximum temperature of the glass window will decrease. In the absence of wind, the average temperature of the glass window is 47.5 °C, and the maximum temperature of the glass window is 77.3 °C. When the wind speed is increased to 10 m/s, the average temperature of the glass window is 37.2 °C, which is decreased by 10.3 °C. The maximum temperature of the glass window is 66.5 °C, which is decreased by 10.8 °C.

The Fig.7 shows the temperature distribution of the water under different wind speeds when the other parameters are the same. As shown in Fig. 6 that the average temperature and the maximum temperature of the water decrease as the wind speed increases. The average temperature of the water inside the volumetric receiver is 35.1 °C and the maximum temperature of the water inside the volumetric receiver is 69.6 °C under the absence of wind; when the wind speed is increased to 10 m/s, the average temperature of water is 33.1 °C, which is decreased by 2.0 °C; the maximum temperature of water is 64.9 °C, which is decreased by 4.7 °C.

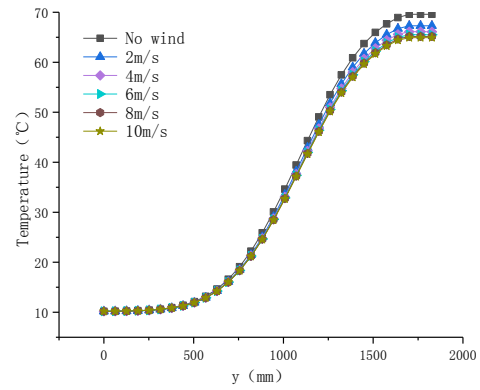
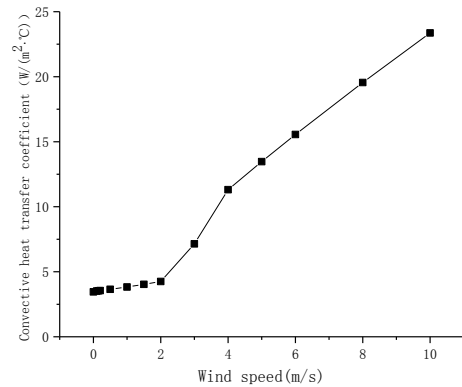
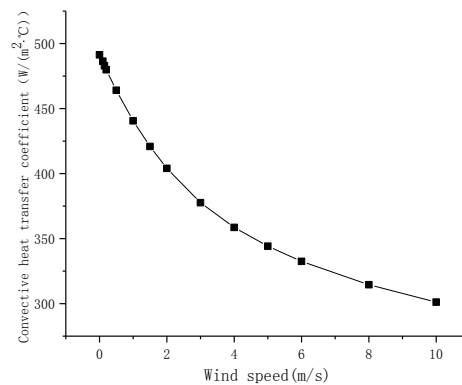


Fig.7 Effect of wind speed on temperature distribution of the water

The Fig.8 shows the effect of the wind speed on the convective heat transfer coefficient of the glass window surface.



(a) The effect of the wind speed on the convective heat transfer coefficient between the glass window and the air



(b) The effect of the wind speed on the convective heat transfer coefficient between the glass window and the water

Fig 8 The effect of the wind speed on the convective heat transfer coefficient

It can be seen from Fig. 8(a) that when the wind speed increases, the convective heat transfer

coefficient between the glass window and the air increases. When the wind speed is 1 m/s, the convective heat transfer coefficient between the glass window and the air is  $3.8 \text{ W}/(\text{m}^2 \cdot ^\circ\text{C})$ . When the wind speed is increased to 10 m/s, the convective heat transfer coefficient between the glass window and the air increases to  $23.4 \text{ W}/(\text{m}^2 \cdot ^\circ\text{C})$ . As shown in Fig.8(b) that when the wind speed increases, the convective heat transfer coefficient between the glass window and the water decreases. When the wind speed is 1 m/s, the convective heat transfer coefficient between the glass window and the water is  $440 \text{ W}/(\text{m}^2 \cdot ^\circ\text{C})$ . When the wind speed is increased to 10 m/s, the convective heat transfer coefficient between the glass window and the water drops to  $301 \text{ W}/(\text{m}^2 \cdot ^\circ\text{C})$ .

Fig.9 shows the effect of wind speed on the thermal efficiency of a volumetric receiver when the other parameters are the same. It can be seen from the figure that as the wind speed increases, the thermal efficiency of the volumetric receiver decreases. When the wind speed increases from 0 m/s to 6 m/s, the thermal efficiency of the volumetric receiver decreases by 6.7 percentage points. When the wind speed is greater than 6m/s, the influence of wind speed on the thermal efficiency of the volumetric receiver reduced. When the wind speed is increased from 6 m/s to 12 m/s, the thermal efficiency of the volumetric receiver is only decreased by 1.2 percentage points.

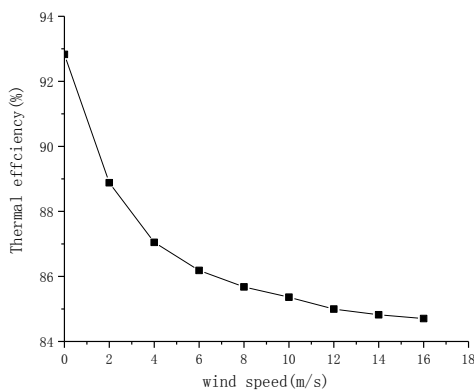


Fig.9 The effect of wind speed on the thermal efficiency

#### 4. CONCLUSIONS

This paper analyzes a volumetric receiver with a

high heat capacity and a one-dimensional unsteady model of volumetric receiver is established. The program was solved based on the MATLAB software. The effect of glass extinction coefficient and wind speed on the thermal performance of the volumetric receiver was analyzed by a one-dimensional unsteady model of volumetric receiver.

The thermal efficiency of the volumetric receiver decreases with the increase of the glass extinction coefficient, and the convective heat transfer coefficient between the glass window and the water increases with the increase of the glass extinction coefficient. When the extinction coefficient of glass increases from  $0 \text{ m}^{-1}$  to  $10 \text{ m}^{-1}$ , the thermal efficiency of the volumetric receiver decreases from 92.2% to 86.1%, and the convective heat transfer coefficient between the glass window and the water rises from  $112 \text{ W}/(\text{m}^2 \cdot ^\circ\text{C})$  to  $331 \text{ W}/(\text{m}^2 \cdot ^\circ\text{C})$ .

The thermal efficiency of the volumetric receiver and the convective heat transfer coefficient between the glass window and the water decrease with the increase of the wind speed. When the wind speed increases from 0 m/s to 10 m/s, the thermal efficiency of the volumetric receiver decreases from 92.8% to 85.4% and the convective heat transfer coefficient between the glass window and water drops from  $440 \text{ W}/(\text{m}^2 \cdot ^\circ\text{C})$  to  $301 \text{ W}/(\text{m}^2 \cdot ^\circ\text{C})$ .

In conclusion, a glass window made of a glass material having a low extinction coefficient can significantly increase the thermal efficiency of the volumetric receiver. Volumetric receiver have higher operating efficiencies when ambient wind speeds are low. The analysis results in this paper can provide reference for the design and operation strategy of volumetric receiver.

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