

# GEOMETRICAL EFFECT ON PERFORMANCE AND CATALYST VOLUME OF METHANE REFORMING WITH CO<sub>2</sub> REACTORS FOR SOLAR THERMOCHEMICAL ENERGY STORAGE

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## ABSTRACT

In CO<sub>2</sub> reforming of methane solar thermochemical energy storage, the endothermic methane reforming with CO<sub>2</sub> reaction is utilized to absorb solar energy. Although a lot of research has been done to enhance the thermochemical performance of the solar driven CO<sub>2</sub> reforming of methane reactor, there is little research conducted investigating the geometrical effect of reactor on the reactor thermochemical performance. Moreover, the catalyst cost is anticipated to be large. Minimizing the required catalyst volume is the key to reduce the capital cost of the CO<sub>2</sub> reforming of methane solar thermochemical energy storage system. But there is not much research investigating the geometrical effect on the catalyst volume. In this paper, a pseudo-homogeneous computational model is used to simulate methane reforming with CO<sub>2</sub> reaction in a tubular packed bed reactor. A parametric study is performed to investigate the geometrical effects of reactor on the reactor performance. The results show that methane conversion as well as outlet gas temperature increase with reactor diameter and/or reactor length increasing while the energy efficiency decreases with reactor diameter and/or reactor length increasing. There is a trade-off between increasing methane conversion and decreasing energy efficiency. As the required catalyst volume increases with reactor size increasing, there is a trade-off between increasing methane conversion and increasing catalyst volume. Another parametric study has been conducted to study the effects of reactor geometries on the required catalyst volume. The results show that the required catalyst volume can be saved by

decreasing the reactor diameter due to enhanced heat transfer.

**Keywords:** Solar thermochemical energy storage, Methane reforming with carbon dioxide, Geometrical effect

## NONMENCLATURE

### Abbreviations

TES	Thermal Energy Storage
STES	Sensible Thermal Energy Storage
LTES	Latent Thermal Energy Storage
TCES	Thermochemical Energy Storage

### Symbols

$c_p$	Specific heat of gas, J/(kg·K)
$D_{eff}$	Effective diffusivity, m <sup>2</sup> /s
$D_p$	Hydraulic diameter, m
$F$	Equivalent particle diameter, m
$E_a$	Flow rate, L/min
$\Delta H$	Activation energy, J/mol
$k_{o,m}$	Heat of reaction, J/kg
$k$	Pre-exponential constant, kg/(m <sup>3</sup> ·s)
$K$	Thermal conductivity, W/(m·K)
$L$	Equilibrium constant
$P$	Reactor length, m
$q_w''$	Pressure, Pa
$\dot{q}'''$	Heat flux, W/(m <sup>2</sup> ·K)
$R_u$	Rate of methanation, kg/(m <sup>3</sup> ·s)
$T$	Universal gas constant, J/(mol·K)
$T_0$	Temperature, °C

$U$	Furnace operating temperature, °C
$V_c$	Heat transfer coefficient, W/(m <sup>2</sup> ·K)
$v$	Catalyst volume, m <sup>3</sup>
$X_{CH_4}$	Velocity, m/s
$Y_{CH_4}$	$X_{CH_4}$ Methane conversion
$\epsilon$	$Y_{CH_4}$ Methane volume fraction
$\eta$	Emissivity of the reactor wall
$\eta_{en}$	Effectiveness factor
$\mu$	Energy efficiency
$\rho$	Viscosity of the gas mixture, Pa·s
	Density of the gas mixture, kg/m <sup>3</sup>

## 1. INTRODUCTION

Solar energy is a renewable and widely-used alternative to the fossil fuel. In order to overcome the drawback of intermittence, thermal energy storage (TES) is used for solar power plants, e.g., using molten salt tanks, as a sensible thermal energy storage (STES), to store solar energy in solar power plants. Besides the STES, latent thermal energy storage (LTES) and thermochemical energy storage (TCES) are the common methods for TES [1]. Compared with the other two, thermochemical energy storage is superior with a higher energy density and the capability of storing energy in reactants at ambient temperature [2, 3]. The principle of a solar thermochemical energy storage system is to store and use solar energy with reversible reactions. Basically, solar energy is stored during the endothermic reaction, which is called as the charging step, and released during the exothermic reaction, which is called as the discharging step. A lot of scholars are currently studying many potential TCES systems with different reactions. But more breakthroughs are required to address the potential catalyst sintering caused by elevated operating temperature and insufficient heat transfer. Ammonia decomposition/synthesis TCES (ammonia-based TCES) is one of the most mature TCES [2, 3]. The charging loop, i.e., absorbing solar energy with ammonia decomposition, has been validated by Lovegrove and Kreetz et al. [4]. Moreover, the discharging loop, i.e., heating steam with ammonia synthesis, by Chen et al. [5-6]. However, there has not been a relatively cheap and safe method validated to store a large amount of the gaseous reactants, i.e., N<sub>2</sub> and H<sub>2</sub>, which constrains the potential of incorporating the ammonia-based TCES with a commercial power plant. CO<sub>2</sub> reforming of methane, as thermochemical energy storage, has been investigated since 1990s [7]. On-sun tests of CO<sub>2</sub> reforming of methane have been conducted at Sun Yat-Sen University

[8] with promising results. Compared with other TCES technologies, CO<sub>2</sub> reforming of methane is superior with a high energy density. Further, the excessive products of hydrogen can be used as a non-carbon fuel. Figure 1 shows a schematic of a CO<sub>2</sub> reforming of methane solar thermochemical energy storage system. As shown in Figure 1, methane (CH<sub>4</sub>) and carbon dioxide (CO<sub>2</sub>) from the storage tank react endothermically by absorbing solar energy. The products of hydrogen (H<sub>2</sub>) and carbon monoxide (CO) flow back to the other storage tank. The stored energy can be released when the hydrogen (H<sub>2</sub>) and carbon monoxide (CO) react exothermically to heat a working fluid for power cycles to generate electricity, e.g., supercritical carbon dioxide (sCO<sub>2</sub>) for a Brayton cycle. A lot of research has been done on CO<sub>2</sub> reforming of methane solar thermochemical energy storage system, most of which focuses on the thermochemical performance of the reactor [8-10]. Recently, Lee et al. [11] studied the effect of the reactor radius on the hydrogen production of a membrane reactor for carbon dioxide reforming of carbon dioxide. However, the geometrical effect of reactor, i.e., reactor diameter and length, on the reactor thermochemical performance including energy efficiency, methane conversion and required catalyst volume are rarely investigated.

The CO<sub>2</sub> reforming of methane solar thermochemical energy storage system, shown in Figure 1, operates in a closed loop. Since there is no regularly recurring expense for feedstock, the cost of the system is mainly determined by the initial capital cost, including the costs of manufacturing material and the catalyst. Nickel-based catalyst is one of the most widely-used catalysts for CO<sub>2</sub> reforming of methane [12]. However, the cost of nickel-based catalyst is still expensive, which need be optimized for the system design. There has not been any investigation performed pertaining saving the catalyst cost of a solar driven methane reforming with CO<sub>2</sub> reactor. In this paper, a simulation model is presented for CO<sub>2</sub> reforming of methane reaction in a tubular packed bed. The model is also used to investigate the geometrical effect of reactor on the reactor performance, e.g., energy efficiency and methane conversion, and required catalyst volume.

## 2. MODELING

A pseudo-homogeneous model [6] is used to simulate the reaction kinetics and thermodynamics of reacting gas in a tubular packed bed. The model utilizes effective properties for fluid and solid phases. Figure 2 shows a schematic of a tubular packed reactor.

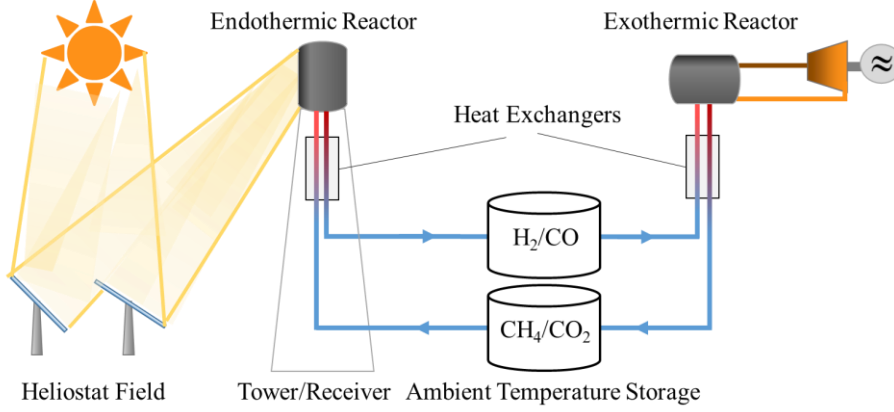


Fig 1 Schematic of a methane reforming thermochemical energy storage system.

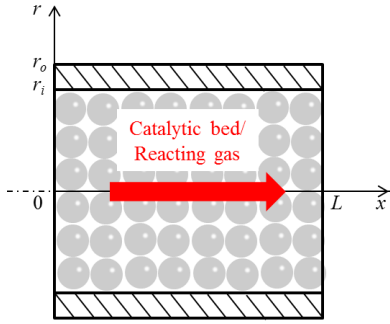
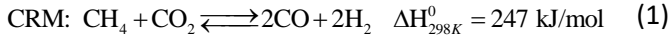
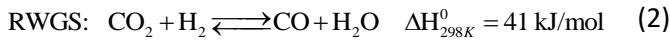


Fig 2 Schematic of a methane reforming with CO<sub>2</sub> reactor.

In this reactor, reacting gas is reacting endothermically (CO<sub>2</sub> reforming of methane reaction) in the catalyst bed. CO<sub>2</sub> reforming of methane consists of two reactions, i.e., the main reaction and the side reaction. The main reaction is the carbon dioxide reforming of methane (CRM):



The side reaction is the reverse water gas shift (RWGS) processes:



The energy conservation equation neglecting the axial conduction is:

$$\rho_g v_g c_{p,g} \frac{\partial T_g}{\partial x} = \frac{1}{r} \frac{\partial}{\partial r} \left( k_{\text{eff}} r \frac{\partial T_g}{\partial r} \right) + \dot{i}''' \Delta H \quad (3)$$

where  $\rho_g$  is the reacting gas density,  $v_g$  is the reacting gas velocity,  $c_{p,g}$  is the reacting gas specific heat capacity,  $\dot{i}'''$  is the reaction rate,  $\Delta H$  is the heat of the reaction, and  $k_{\text{eff}}$  is the effective thermal conductivity. The boundary conditions for Eq. (3) are:

$$T_g(r, x=0) = T_{g,\text{in}} \quad (4)$$

$$k_{\text{eff}} \frac{\partial T_g}{\partial r} (r = r_1, x) = U_o [T_g(r = r_1, x) - T_w(x)] = q_w'' \quad (5)$$

where  $U_o$  is the overall heat transfer coefficient at the catalyst bed outer wall,  $T_w$  is the wall temperature, and

$q_w''$  is the heat flux at the reactor wall. The overall heat transfer coefficient  $U_o$  accounts for the thermal conduction through the reactor wall. The heat flux at the reactor wall is determined by the radiation from a furnace outside of the reactor and heat loss to the ambient:

$$q_w'' = \varepsilon \sigma (T_f^4 - T_w^4) + h_{\text{loss}} (T_a - T_w) \quad (6)$$

where  $T_f$  is the furnace radiant surface temperature,  $h_{\text{loss}}$  is the heat transfer coefficient for the heat loss, and  $T_a$  is the ambient temperature. Note that,  $T_f = T_0 + 10 \text{ K}$ , where  $T_0$  is the operating temperature for the furnace.

The mass conservation equation neglecting the axial diffusion is:

$$\rho_g v_g \frac{\partial X_{\text{CH}_4}}{\partial x} = \rho_g D_{\text{eff}} \frac{1}{r} \frac{\partial}{\partial r} \left( r \frac{\partial X_{\text{CH}_4}}{\partial r} \right) + \dot{i}''' \quad (7)$$

where  $X_{\text{CH}_4}$  is the methane conversion. The corresponding boundary conditions for mass conservation are:

$$X_{\text{CH}_4}(r, x=0) = X_{\text{CH}_4,\text{in}} \quad (8)$$

$$\left. \frac{\partial X_{\text{CH}_4}}{\partial r} \right|_{r_i} = 0 \quad (9)$$

In the model, the reaction rate  $\dot{i}'''$  is determined by the kinetics of CRM reaction as RWGS reaction is assumed to be always at equilibrium. The chemical reaction kinetics is modeled based on the basic reaction model [13]:

$$\dot{i}''' = \eta k_{o,m} \exp\left(\frac{-E_a}{R_u T}\right) \left[ P_{\text{CH}_4} P_{\text{CO}_2} - K_C^{-1} P_{\text{CO}}^2 P_{\text{H}_2}^2 \right] \quad (10)$$

where the effectiveness factor  $\eta$  accounts for the reactant concentration gradient within the catalyst particle. The equilibrium constant  $K_C$  based on the data from [14] is calculated as:

$$K_C = \exp(34.225 - 31299/T_g) \quad (11)$$

For the RWGS reaction (Equation 2), the chemical reaction kinetics is modeled as:

$$P_{CO_2}P_{H_2} = K_R^{-1}P_{CO}^2P_{H_2O}^2 \quad (12)$$

where  $K_R$  is the equilibrium constant for the reaction, which is calculated based on the data from Callaghan [15]. The reactor bed is filled with Ni/Al<sub>2</sub>O<sub>3</sub> (Ni-15 wt%) catalyst with kinetic parameters listed in Table 1.

Table 1 The kinetic parameters for the model input

Activation energy, $E_a$ (J/mol)	Pre-exponential constant, $k_{o,m}$ (kg/m <sup>3</sup> ·s)
$5.8 \times 10^3$	$1.36 \times 10^9$

The energy efficiency of the reactor  $\eta_{en}$  can be estimated as:

$$\eta_{en} = Q_r / (Q_r + Q_{loss}) \quad (13)$$

where  $Q_r$  is the rate at which energy is transferred to the reacting gas and  $Q_{loss}$  is the heat loss rate from the reactor.

### 3. RESULTS AND DISCUSSIONS

#### 3.1 Model Validation

A FORTRAN code is developed to numerically solve the governing equations with a finite difference algorithm. The grids independency has been validated by setting the same model with more than twice of the grids. The results including the outlet gas temperature and conversion for the two different grids are similar with difference of 1%. In order to validate the model, the model generated methane conversions  $X_{CH_4}$  for different furnace operating temperature  $T_0$  are compared with experimental results from Lu et al. [10]. The properties and parameters used for model input including the inlet gas flow rate  $F_{in}$ , methane volume fraction  $Y_{CH_4}$ , inlet gas temperature  $T_{g,in}$ , furnace operating temperature  $T_0$ , reactor length  $L$ , reactor inner diameter  $D_i$ , and reactor wall thickness  $W$  ( $W=r_o-r_i$ ) are listed in Table 2.

Table 2 Properties of a sample case for the model

$F_{in}$ (L/min)	$Y_{CH_4}$	$T_{g,in}$ (°C)	$T_0$ (°C)	$L$ (m)	$D_i$ (cm)	$W$ (cm)
4	0.5	550	800	0.2	2.6	0.2

Figure 3 shows the comparison of model generated methane conversion  $X_{CH_4,m}$  and experimental measured one  $X_{CH_4,exp}$  from literature [10]. As shown in Figure 3, the model generated results are in good agreement with the experimental results with the maximum deviation of 11% at  $T_0=750$  °C. Based on the validation of the model, parametric studies were performed to investigate the effect of reactor geometries, i.e., reactor inner diameter  $D_i$  and reactor length  $L$ , on the performance of the reactor, i.e., energy efficiency  $\eta$  and methane conversion

$X_{CH_4}$ . Moreover, the effect of reactor geometries on the required catalyst volume is explored as well.

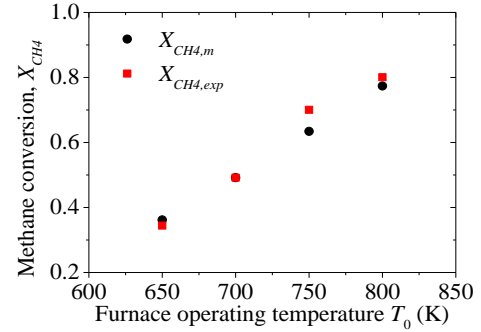


Fig 3 Comparison of model generated methane conversion  $X_{CH_4,m}$  and experimental measured one  $X_{CH_4,exp}$  [10].

#### 3.2 Geometrical Effect on Reactor Performance

##### 3.2.1 Effect of Diameter

For the solar driven CO<sub>2</sub> reforming of methane reactor, the performance is expected to be affected by the reactor diameter since both residence time and heat transfer depends on the reactor diameter. A parametric investigation is performed to study the effect of reactor inner diameter  $D_i$  (see Figure 2) on the reactor performance. In this investigation, the inner diameter  $D_i$  is varied from 1.5 to 3.5 cm while the reactor length is fixed to be 0.4 m. Other fixed conditions i.e., the inlet gas flow rate  $F_{in}$ , the CH<sub>4</sub> volume fraction  $Y_{CH_4}$ , the gas inlet temperature  $T_{g,in}$ , the furnace operating temperature  $T_0$ , the reactor length  $L$  and the reactor wall thickness  $W$ , are fixed and listed in Table 2. Figure 4 shows methane conversion  $X_{CH_4}$  and outlet gas temperature  $T_{g,out}$  for different reactor inner diameters  $D_i$ . As shown in Figure 4, both methane conversion  $X_{CH_4}$  and outlet gas temperature  $T_{g,out}$  increase with reactor diameter  $D_i$  increasing. That is because the residence time increases with reactor diameter  $D_i$  increasing. As  $T_{g,out}$  approaches to a high temperature  $\sim 790$  °C, the increasing rates of both  $X_{CH_4}$  and  $T_{g,out}$  become quite moderate. That is because the heat loss, affected by the temperature difference between the reactor and the ambient, increases with reactor temperature increasing. Meanwhile the radiation from the furnace, determined by the temperature difference between the reactor and the furnace, decreases with reactor temperature increasing. Figure 5 shows the heat loss  $Q_{loss}$  and energy efficiency  $\eta_{en}$  of the reactor for different reactor inner diameters  $D_i$ . As expected, the heat loss  $Q_{loss}$  (in Figure 5) increases with  $D_i$  increasing because of increasing surface area. Although heat transferred to the reacting

gas  $Q_r$  also increases with inner diameter  $D_i$  increasing, the energy efficiency  $\eta_{en}$  (in Figure 5) decreases with  $D_i$  increasing. Therefore, there is a trade-off between increasing  $X_{CH_4}$  and decreasing  $\eta_{en}$  when  $D_i$  is varied.

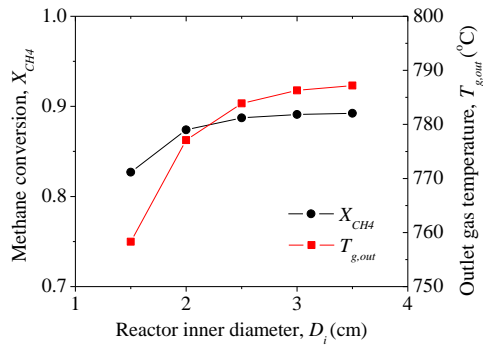


Fig 4 Methane conversion  $X_{CH_4}$  and outlet gas temperature  $T_{g,out}$  as functions of inner diameter  $D_i$ .

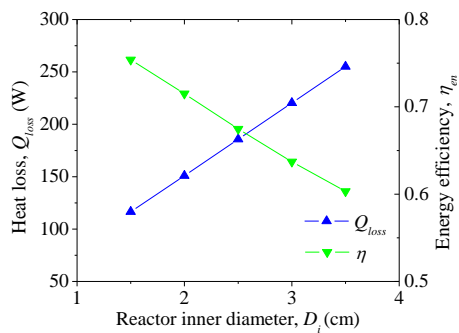


Fig 5 Heat loss  $Q_{loss}$  and energy efficiency  $\eta_{en}$  of the reactor as functions of reactor inner diameter  $D_i$ .

### 3.2.2 Effect of Length

The reactor length  $L$  is also a crucial factor affecting the reactor performance since the residence time depends on the reactor length  $L$ . A parametric investigation is performed to study the effect of the length  $L$  on the reactor performance. In this investigation, the reactor length  $L$  is varied from 10 to 50 cm while the diameter  $D_i$  is fixed to be 2.5 cm. Other fixed conditions listed in Table 2. Figure 6 shows methane conversion  $X_{CH_4}$  and outlet gas temperature  $T_{g,out}$  for different reactor length  $L$ . Similar to the case of increasing  $D_i$  (in Figure 6), both  $X_{CH_4}$  and  $T_{g,out}$ , shown in Figure 6, increase with  $L$  increasing due to longer residence time. Figure 7 shows the heat loss  $Q_{loss}$  and energy efficiency  $\eta_{en}$  of the reactor for different reactor length  $L$ . As shown in Figure 7,  $Q_{loss}$  increases with  $L$  increasing while  $\eta_{en}$  decreases with  $L$  increasing because of heat loss surface area increasing. There is a trade-off between increasing  $X_{CH_4}$  and decreasing  $\eta_{en}$  when  $L$  is varied.

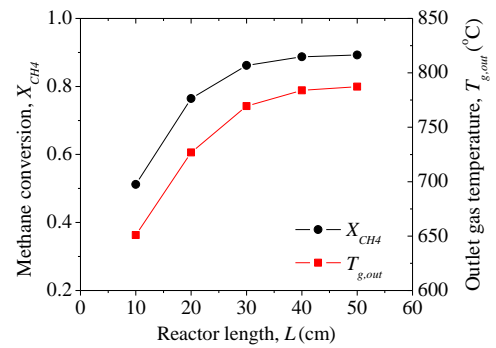


Fig 6 Methane conversion  $X_{CH_4}$  and outlet gas temperature  $T_{g,out}$  as functions of reactor length  $L$ .

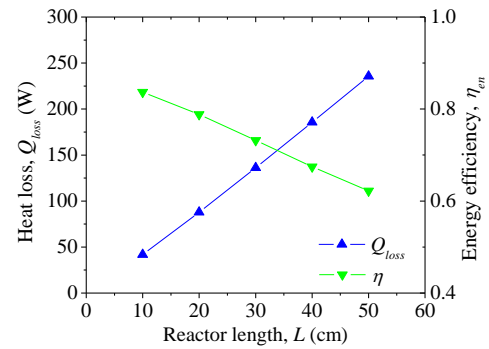


Fig 7 Heat loss  $Q_{loss}$  and energy efficiency  $\eta_{en}$  as functions of reactor length  $L$ .

### 3.3 Geometrical Effect on Required Catalyst Volume

Based on the previous discussion, the methane conversion and the outlet gas temperature can be increased by increasing reactor diameter and/or reactor length, which increases the required catalyst volume as well. In this section, the effect of geometries on the required catalyst volume is investigated by varying both reactor inner diameter  $D_i$  and reactor length  $L$  simultaneously while both the methane conversion  $X_{CH_4}$  and outlet gas temperature  $T_{g,out}$  are fixed. Table 3 lists all the fixed conditions. Figure 8 shows the reactor length  $L$  and required catalyst volume  $V_c$  for different reactor inner diameter  $D_i$ . As shown in Figure 8,  $L$  increases with  $D_i$  decreasing. But  $V_c$  decreases with  $D_i$  decreasing. That is because the heat transfer is enhanced by decreasing  $D_i$ . Thus, smaller reactor diameter is preferred in saving catalyst cost to achieve a fixed methane conversion  $X_{CH_4}$ .

Table 3 Fixed conditions for studying the effect of geometries on required catalyst volume

$F_{in}$ (L/min)	$Y_{CH_4}$	$T_{g,in}$ ( $^{\circ}C$ )	$T_0$ ( $^{\circ}C$ )	$W$ (cm)	$X_{CH_4}$	$T_{g,out}$ ( $^{\circ}C$ )
4	0.5	550	800	0.2	0.89	784

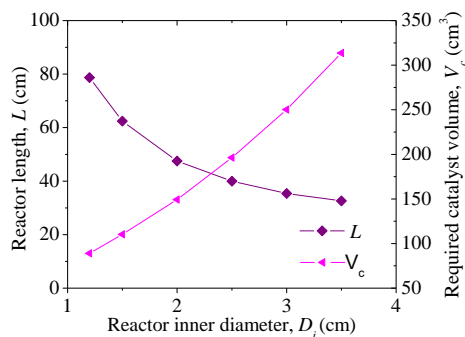


Fig 8 Reactor length  $L$  and required catalyst volume  $V_c$  as functions of reactor diameter  $D_i$ .

#### 4. CONCLUSIONS

This paper has investigated performance and required catalyst volume of a solar driven methane reforming with  $\text{CO}_2$  reactor. A pseudo-homogeneous model has been used to simulate  $\text{CO}_2$  reforming of methane reaction in a tubular packed bed reactor. A parametric study was conducted to investigate the geometrical effects on the reactor performance, i.e., methane conversion and energy efficiency. The results show that both methane conversion and outlet gas temperature increase with reactor diameter and/or reactor length increasing while the energy efficiency decreases with reactor diameter and/or reactor length increasing. There is a trade-off between increasing the methane conversion and decreasing the energy efficiency. Similarly, there is a trade-off between increasing the methane conversion and increasing the required catalyst volume since the required catalyst volume increase with reactor diameter and/or reactor length increasing. Another parametric study is needed to investigate the effect of geometries on the desired catalyst volume when methane conversion is fixed. The results show that the required catalyst volume can be saved by decreasing the reactor diameter due to enhanced heat transfer. The analysis presented here provides a baseline for further design refinement and economic analysis.

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