

A heat-driven thermoacoustic heat pump with a single direct-coupling configuration capable of utilizing medium/low-grade heat for domestic applications[#]

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ABSTRACT

This paper proposed a heat-driven thermoacoustic heat pump system capable of utilizing medium/low-grade heat for heating supply in domestic applications. The system consists of one simple thermoacoustic energy-conversion unit with a direct-coupling configuration, which greatly reduces the system complexity compared to the traditional multi-stage thermoacoustic systems. The dimensional parameters of the system were optimized under nominal conditions, with heat-sink and heat-source temperatures of 55 °C and 7 °C. Simulation results show that the proposed system can obtain a heating capacity of 5.7 kW and an overall coefficient of performance of 1.40 at nominal conditions. Economic performance shows annual fuel energy savings and energy cost savings for individual systems are 20.3 MWh/year and 675 \$/year. The environmental assessments show that the proposed system can displace CO₂ emissions amounting to 3.72 tCO₂/year. Exergy loss of each component was then given better to understand the energy conversion processes of the system. Moreover, system performance under different heat-source and heat-sink temperatures was studied.

Keywords: Thermoacoustic heat pump; Building energy; Low/medium-grade heat recovery; Domestic heating; Energy saving; Energy conversion technology.

NONMENCLATURE

Symbols

AE_{fric} flow friction losses, W

| | |
|--------------|--|
| AE_{Qw} | non-ideal heat transfer losses between the gas and the solid, W |
| AE_{Qx} | axial heat flow losses, W |
| C_s | energy cost savings, \$ |
| COP | coefficient of performance |
| c_{ng} | price of natural gas, \$/kWh |
| f | frequency, Hz |
| f_{ng} | CO ₂ emission factor of natural gas, kgCO ₂ /kWh |
| F | viscous pressure gradient |
| P | pressure amplitude, kPa |
| P_m | mean pressure, MPa |
| Pr | pressure ratio at the inlet of engine stage |
| Q_{demand} | demand heat supply, kW |
| $Q_{e,in}$ | input heating power of the engine stage, kW |
| $Q_{e,out}$ | output heating capacity of the engine stage, kW |
| $Q_{hp,in}$ | input heating power of the heat pump stage, kW |
| $Q_{hp,out}$ | output heating capacity of the heat pump stage, kW |
| Q_{out} | output heating capacity of the system, kW |
| q | instantaneous axial heat flux, W/m ² |
| q_F | heating load index, W/m ² |
| q_{ng} | calorific value of piped natural gas, MJ/m ³ |
| q_w | heat flux between gas and solid |
| q_x | heat flux between gas and gas or between solid and solid |
| S_{mean} | per capita housing area, m ² /person |
| S_{family} | household size, person/household |
| T | temperature, K |

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| | |
|-----------------------|---------------------------------|
| T_h | heating temperature, K |
| T_{source} | heat-source temperature, K |
| T_{sink} | heat-sink temperature, K |
| Greek letters | |
| η | relative Carnot efficiency, % |
| η_{boi} | efficiency of boiler, % |
| τ_{anu} | annual operating time, hour |
| uA | volumetric flow rate |
| Special symbol | |
| $ $ | magnitude of the complex number |
| ∇ | gradient of the complex number |
| Abbreviations | |
| CT | cavity structure |
| ER | emission reduction |
| FES | fuel energy savings |
| HHX | high-temperature heat exchanger |
| HSHX | heat-source heat exchanger |
| REG | regenerator |
| RT | resonant tubes |
| SHX | heat-sink heat exchanger |
| TBT | thermal buffer tube |

1. INTRODUCTION

Thermoacoustic technology, as an emerging energy conversion technology, can be used for heating [1], cooling [2], or power generation [3]. This technology is not only environmentally friendly due to the use of pollution-free working gas, but also has a simple structure and contains no mechanical moving parts for a long fatigue life [4]. Current research on thermoacoustic heat pumps focuses on Stirling-type thermoacoustic heat pumps. In 2020, Cheng et al. proposed a beta-type Stirling heat pump driven by a linear motor which achieved a coefficient of performance (COP) of 1.8 [5]. In 2021, a linear-compressor-driven free-piston Stirling heat pump presented by Wang et al. achieved a COP of 2.41 [6]. Few studies have been reported on heat-driven thermoacoustic heat pumps. In 2020, Sun et al. proposed a free-piston Stirling heat pump driven by a Stirling engine, achieving a heating capacity of 6 kW and a COP of 1.8 [7]. While numerous research has reported high performance, the thermoacoustic heat pump is still in the early stages of development and the demonstrators reported are not viable for domestic applications due to the system complexity and the necessary use of high-temperature heat sources (>900 K). In this paper, we propose a first thermoacoustic heat pump capable of utilizing low/medium-grade waste heat, in particular

aiming at domestic heating. The thermoacoustic heat pump consists of one simple thermoacoustic energy-conversion unit and has no moving parts. First, a numerical study including system performance and energy loss analysis was conducted to explore the operating characteristics. Then, the heat pump performance under different heat sink/source temperatures was investigated to assess the utility of the system. Finally, some conclusions are presented.

2. SYSTEM DESCRIPTION

2.1 Configuration

Fig. 1 presents the schematic of a heat-driven thermoacoustic heat pump. The system includes an engine unit, a heat pump unit, and a gas resonator unit in a loop. The engine unit consists of a heat-sink heat exchanger (SHX_e), a regenerator (REG_e), a high-temperature heat exchanger (HHX_e), and a thermal buffer tube (TBT_e). The cooler unit consists of a heat-sink heat exchanger (SHX_h), a regenerator (REG_h), a heat-source heat exchanger (HSHX_h), and a thermal buffer tube (TBT_h). *e* is for the engine stage and *h* is for the heat pump stage. The system works as follows: self-excited thermoacoustic oscillation begins and the conversion from heat to acoustic power occurs when the axial temperature gradient generated in the regenerator of the engine exceeds a critical value. The amplified acoustic power is used to drive the heat pump unit to pump heat from the heat source to the heat sink. Table 1 shows the geometric dimensions of the main components of the system.

2.2 Simulation model description

In this study, the numerical simulation of the heat-driven thermoacoustic heat pump is based on the SAGE program, which is widely used in modeling thermoacoustic devices [8-10].

Some important evaluating indicators are of interest. The coefficient of performance (COP) of the system can be expressed as

$$COP = \frac{Q_{out}}{Q_{e,in}} = \frac{Q_{e,out} + Q_{hp,out}}{Q_{e,in}} \quad (1)$$

where $Q_{e,out}$ and $Q_{hp,out}$ are the output heat from the SHX_e and SHX_h, respectively. $Q_{e,in}$ is the input heat to HHX_e.

Eq. (2) gives the relative Carnot efficiency of performance of the system,

$$\eta = \frac{COP}{\frac{T_{sink} + T_h - T_{sink}}{T_h} \times \frac{T_{sink}}{T_{sink} - T_{source}}} \quad (2)$$

where T_{sink} and T_{source} are the temperatures of the heat sink and heat source, respectively.

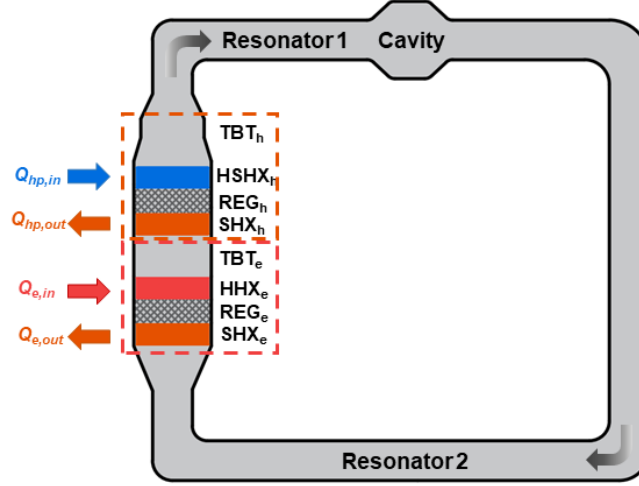


Fig.1. Schematic of a heat-driven thermoacoustic heat pump

Table 1

Dimensions of the components in each subunit.

| Subunit | Parts | Diameter (mm) | Length (mm) | Other dimensions |
|---------------|-------------------|---------------|-------------|---|
| Engine | SHX _e | 150 | 33 | Shell tube type, 11% in porosity, 1 mm in internal diameter |
| | REG _e | 150 | 40 | 76% in porosity, 50 μm in wire diameter |
| | HHX _e | 150 | 33 | Shell tube type, 11% in porosity, 1 mm in internal diameter |
| Heat-pump | TBT _e | 150 | 100 | 7 mm in wall thickness |
| | SHX _h | 150 | 33 | Shell tube type, 11% in porosity, 1 mm in internal diameter |
| | REG _h | 150 | 35 | 71% in porosity, 50 μm in wire diameter |
| | HSHX _h | 150 | 33 | Shell tube type, 11% in porosity, 1 mm in internal diameter |
| Gas resonator | TBT _h | 90 | 50 | 7 mm in wall thickness |
| | RT ₁ | 54 | 2150 | 1E-3 in relative roughness |
| | CT | 115 | 500 | 1 mm in wall thickness |
| | RT ₂ | 54 | 9650 | 1E-3 in relative roughness |

In addition to heating capacity and system efficiency, the fuel energy saving (FES), annual energy cost saving (C_s), and potential CO₂ emission reduction (ER) of this system have been explored to show the environmental and economic potentials of the system. FES is expressed as follows:

$$FES = \frac{Q_{out}}{\eta_{boi}} \times \tau_{anu} \quad (3)$$

where η_{boi} and τ_{anu} are the efficiency of the conventional boiler and annual operating time, respectively. η_{boi} is taken here to be 82% [11]. τ_{anu} can be simply calculated as $\tau_{anu} = Day_h \times 24 h$. The

annual heating days, Day_h , taking Beijing as an example, are generally 120 days [12].

$$C_s = \frac{Q_{out}}{\eta_{boi} \times q_{ng}} \times c_{ng} \times \tau_{anu} \quad (4)$$

where c_{ng} is the price of piped natural gas in China, which is 1.047 \$/m³ according to the latest data [13]. q_{ng} , the calorific value of piped natural gas, is required to be greater than 31.4 MJ/m³ in the relevant Chinese norms [14].

$$ER = \frac{Q_{out}}{\eta_{boi}} \times f_{ng} \times \tau_{anu} \quad (5)$$

where f_{ng} is the CO₂ emission factor of natural gas, 0.1836 kgCO₂/kWh [15].

3. SIMULATION RESULTS

3.1 Performance in nominal condition of the system

Table 2 gives the simulation results from SAGE in the nominal conditions of the system. The nominal conditions are based on the domestic heating applications: heat sink temperature is set at 55 °C, which is reported as the minimum temperature to prevent the harmful bacteria in the hot water supply [16]; heat source temperature is set at 7 °C according to the industrial standard in heat pump field [17]; the heating temperature in engine stage is chosen as 300 °C due to the intention of utilizing medium/low-grade temperature heat. The nominal heating capacity of 5.7 kW_{th} is chosen according to the typical domestic heating

supply in China: taking ordinary low-rise residential buildings with energy-saving measures in Chinese towns as examples, the demand heat supply, Q_{demand} is calculated as follows:

$$Q_{demand} = S_{mean} \times S_{family} \times q_F \quad (6)$$

where S_{mean} , S_{family} , and q_F are the per capita housing area in Chinese towns, the household size, and the heating load index, respectively. Their values are 39.8 m²/person [18], 2.62 person/household [19], and 55 W/m² [20] from relevant reports and specifications. A nominal heating capacity of 5.7 kW_{th} is thus obtained from Eq. 6. A coefficient of performance (COP) of 1.40 and a relative Carnot coefficient of performance (η) of 39.9% are obtained as well. Additionally, the cost savings and emissions assessments indicate that, this system has the potential to save 20.3 MWh of fuel energy consumption, 675 \$ for an ordinary family, and to displace around 3.72 tons of CO₂ emission per year.

Table 2
Simulation results in nominal condition of the system

| Symbol | Parameter | Value |
|--------------|--|-------|
| P_m | Mean pressure (MPa) | 10 |
| Pr | Pressure ratio at the inlet of engine stage | 1.07 |
| T_h | Heating temperature of the engine stage (K) | 573 |
| T_{source} | Temperature of the heat source (K) | 280 |
| T_{sink} | Temperature of the heat sink (K) | 328 |
| f | Working frequency (Hz) | 72.2 |
| $Q_{e,in}$ | Input heating power in engine stage (kW) | 4.10 |
| Q_{out} | Output heating capacity of the system (kW) | 5.70 |
| COP | Coefficient of performance of the system | 1.40 |
| η | Relative Carnot efficiency of the system | 39.9% |
| FES | Annual fuel energy saving (MWh/year) | 20.3 |
| C_s | Annual energy cost saving (\$/year) | 675 |
| ER | Annual potential CO ₂ emission reduction (tCO ₂ /year) | 3.72 |

3.2 Exergy losses analysis of the system

Exergy losses analysis allows for an accurate assessment of the system performance and provides guidance for subsequent improvement. The usual losses include flow friction losses (AE_{fric}), non-ideal heat transfer losses (AE_{Qw}) between the gas and the solid, and axial heat flow losses (AE_{Qx}). They are respectively calculated as

$$AE_{fric} = -T_0 \times \oint_{dt} \int_{dx} \frac{uAF}{T} \quad (6)$$

$$AE_{Qw} = -T_0 \times \oint_{dt} \int_{dv} \frac{q_w \cdot \nabla T_w}{T^2} \quad (7)$$

$$AE_{Qx} = -T_0 \times \oint_{dt} \int_{dv} \frac{q_x \cdot \nabla T_x}{T^2} \quad (8)$$

where uA and F are the volumetric flow rate and the viscous pressure gradient, q_w and ∇T_w are the heat flux and the temperature gradient between gas and solid, q_x and ∇T_x are the heat flux and the temperature gradient between gas and gas or between solid and solid.

Fig. 2 presents the exergy losses of the different components of this heat pump. The acoustic impedance is large in the regenerator, so the non-ideal heat transfer losses and axial heat flow losses account for most of the exergy losses. And in the resonant tubes, most losses come from the flow friction losses because of the large

tube length. The optimization of these components can improve the system performance.

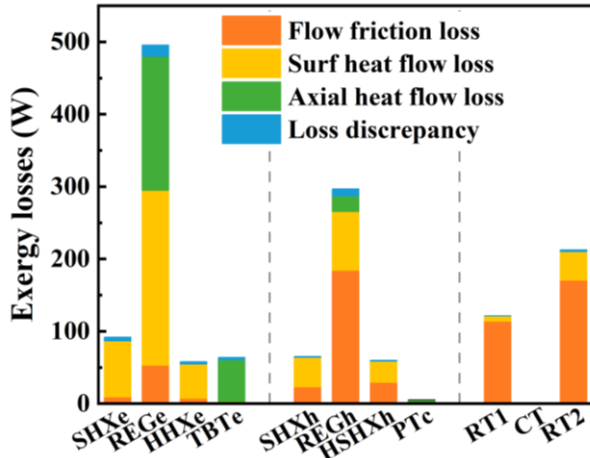


Fig. 2. Exergy losses analysis of the system in different components.

3.3 Effect of the heat-sink and heat-source temperatures

The operating conditions of domestic heat pumps are determined by environmental factors including heat-sink and heat-source temperatures, which significantly affect the heating performance of thermoacoustic heat pumps. Fig. 3 (a-d) show the effect of the heat-sink temperature on the heating performance under different heat-source temperature. The heat-source temperature varies between 260 K and 310 K, reflecting the variations in system performance over the seasons. The heat-sink temperature varies between 298 K and 363 K, covering the range of applications from low-temperature underfloor space heating to the provision of domestic hot water.

Generally, the input heating power, output heating capacity, and COP increase as the temperature difference between the heat-sink and heat-source decreases, while the η is on the contrary. Exceptionally, the variation of η at the heat-source temperature of 260

K, 270 K, and 280 K proves the existence of an optimal heat-sink temperature for the relative Carnot efficiency of the system. The thermoacoustic heat pump provides stable COP values over the temperature range considered, varying between 1.1 and 1.5 over most of the temperature range, which verifies that the proposed heat pump system supplies heat stably in a wide temperature range. Especially in the typical domestic heating supply temperature range of 50-70 °C, the proposed heat pump system can pump several kilowatts (1-11 kW) of heat from a heat source of 260 K to 310 K with remarkable efficiency.

4. CONCLUSION

A heat-driven thermoacoustic heat pump utilizing medium/low-grade heat for domestic heating applications has been studied in this paper. Numerical results prove the possibilities of practical applications with the heating capacity of 5.7 kW and the overall coefficient of performance (COP) of 1.40. Meanwhile, economic and environmental friendliness are demonstrated with the potential to save 20.3 MWh of fuel energy consumption, 675\$ for an ordinary family, and to displace around 3.72 tons of CO₂ emission per year. Exergy losses analysis was further studied better to understand the energy conversion processes of the system. Moreover, influences of the heat-source and heat-sink temperatures were investigated to evaluate the system's adaptability to the varying operating conditions. In the future, a corresponding testbed will be established, and experimental work will be conducted to verify the simulation results.

ACKNOWLEDGEMENT

This work is supported by the National Natural Science Foundation of China (No. 51976230 and 51876213) and Leading Project A of Chinese Academy of Sciences (No. XDA21080300).

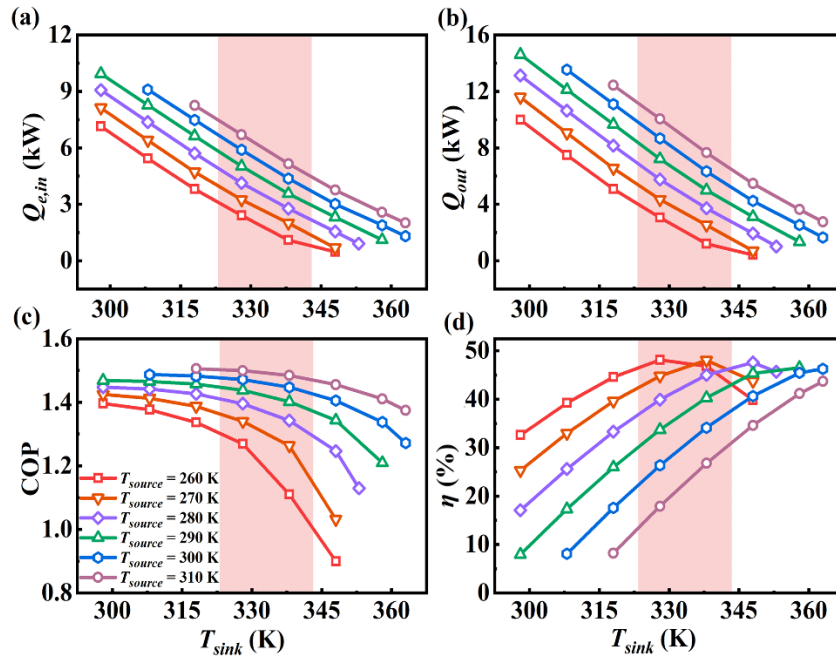


Fig. 3. Effect of the heat-sink and heat-source temperature on system performance. The highlighted area in pink relates to the typical domestic heating supply temperature range of 50-70 °C.

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