

# Study on reasonable production allocation method of CO<sub>2</sub> assisted gravity flooding in low permeability reservoir considering pressure sensitivity effect

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## ABSTRACT

There is a large amount of residual oil in the high part of the reservoir and the recovery rate is low when the high dip angle and low permeability reservoir is developed by water flooding. The use of CO<sub>2</sub> assisted gravity flooding can make full use of the geological characteristics of high dip angle and effectively improve the recovery degree of this kind of reservoir. However, because the influence of CO<sub>2</sub> on the physical properties of crude oil is much greater than the influence of water on the physical properties of crude oil, the seepage process of fluid in the process of CO<sub>2</sub> flooding is more complex, so it is necessary to study the reasonable production allocation optimization of CO<sub>2</sub> gravity flooding in low permeability reservoirs. Firstly, according to the relationship between the pressure at any point in the reservoir and the minimum miscible pressure (MMP), the miscible and immiscible models of CO<sub>2</sub> gravity flooding in low permeability reservoirs considering the pressure sensitivity effect are established respectively. Secondly, Python is used to solve the model, and the influence of pressure sensitivity coefficient, formation dip angle, injection- production well spacing and gas injection speed on reservoir allocation is analyzed. Finally, combined with the existing work system method and the production increase multiple method, compared with the calculation results of this model, the tNavigator software is used to predict the recovery rate of the three methods. The results show that this method has a good development effect on the reasonable production allocation of the reservoir, and the recovery rate of the reservoir is relatively high. The

research results have a good reference for the development of this kind of low permeability reservoir.

**Keywords:** high dip and low permeability reservoir, CO<sub>2</sub> displacement, filtration theory, pressure sensitivity effect, reasonable production allocation

## NONMENCLATURE

### Abbreviations

MMP Minimum miscibility pressure

### Symbols

$q$	the oil production of oil well (m <sup>3</sup> /d)
$K$	formation permeability (mD)
$B$	the stratum width (m)
$h$	the thickness of stratum (m)
$\mu_m$	the fluid viscosity in the miscible region (mPa·s)
$P$	formation pressure (MPa)
$\rho_m$	the fluid density in the miscible region (kg·m <sup>-3</sup> )
$g$	gravity coefficient (N/kg)
$\theta$	formation dip angle (°)
$\lambda_m$	the starting pressure gradient of the fluid in the miscible region (MPa/m)
$P_{mm}$	the minimum miscibility pressure (MPa)
$P_{iwf}$	the bottom hole pressure of the gas injection well (MPa)
$X_m$	the length of the miscibility zone (m)
$\mu_g$	the viscosity of CO <sub>2</sub> gas (mPa·s)

$C$	the concentration of CO <sub>2</sub> (decimal)
$\mu_o$	the viscosity of oil (mPa·s)
$\rho_g$	the density of CO <sub>2</sub> (kg·m <sup>-3</sup> )
$\rho_o$	the density of oil (kg·m <sup>-3</sup> )
$v$	seepage velocity (m·s <sup>-1</sup> )
$\xi$	the velocity coefficient of particle capture (m <sup>-1</sup> )
$D$	the diffusion coefficient of CO <sub>2</sub> in crude oil (m <sup>2</sup> /s)
$\beta$	the adsorption velocity coefficient of particles on the rock surface (s <sup>-1</sup> )
$K_o$	original formation permeability (mD)
$M$	pressure-sensitive coefficient (MPa <sup>-1</sup> )
$P_i$	original formation pressure (MPa)
$a$	positive real numbers (decimal)
$b$	positive real numbers (decimal)
$k_{ro}$	the relative permeability of oil phase (decimal)
$\mu_{io}$	the viscosity of oil phase in immiscible region (mPa·s)
$\rho_{io}$	the oil phase density in immiscible region (kg·m <sup>-3</sup> )
$\lambda_{io}$	the starting pressure gradient of oil phase in immiscible region (MPa/m)
$\varphi$	porosity (decimal)
$S_o$	oil saturation (decimal)
$k_{rg}$	the relative permeability of gas phase (decimal)
$\lambda_g$	the starting pressure gradient of gas phase in immiscible region (MPa/m)
$B_g$	the volume coefficient of CO <sub>2</sub> (m <sup>3</sup> /m <sup>3</sup> )
$B_o$	the volume coefficient of oil (m <sup>3</sup> /m <sup>3</sup> )
$R_s$	the solubility of CO <sub>2</sub> in oil (m <sup>3</sup> /m <sup>3</sup> )
$S_g$	gas saturation (decimal)
$S_{or}$	residual oil saturation (decimal)
$Y_g$	the proportion of CO <sub>2</sub> component in oil phase (decimal)
$\alpha$	a constant related to temperature and pressure (decimal)
$F_g$	the ratio of the volume of CO <sub>2</sub> under standard conditions to the volume under reservoir conditions (m <sup>3</sup> /m <sup>3</sup> )
$F_o$	the ratio of the volume of oil under reservoir temperature and 0.1MPa pressure to the volume under reservoir volume (m <sup>3</sup> /m <sup>3</sup> )
$Q(t)$	the total flow through the seepage section (m <sup>3</sup> )

$X_{im}$	the length of the immiscible zone (m)
$L$	the injection-production well spacing (m)

## 1. INTRODUCTION

With the gradual increase of the contradiction between supply and demand of oil and gas resources, the development of low permeability reservoirs has become the only way. Low permeability reservoir resources account for a large proportion of the total oil and gas resources. More than 40 countries in the world have evaluated the reserves of low permeability reservoirs, and the results show that the recoverable amount is about 483×108t [1]. The proportion of low permeability oil and gas resources in China has reached 49 % of the total oil and gas resources, of which the proven reserves are about 160×108t [2,3]. In the development of water flooding in high dip and low permeability fault block reservoirs, there is a large amount of residual oil in the high part and corner of the reservoir, and the recovery rate is low [4]. The top gas injection flooding is an effective development method for this reservoir. Compared with other gases, CO<sub>2</sub> is easier to dissolve with crude oil, and its critical temperature and pressure are also lower [5]. Its physical and chemical properties determine that its displacement mechanism is mainly to reduce the interfacial tension of crude oil and reduce the displacement resistance [6]; reduce the viscosity of crude oil [7]; expanding the volume of crude oil [8]; extraction and vaporization of light hydrocarbons in crude oil [9]; pressure drop causes dissolved gas flooding [10]; acid solution plugging effect, improve the injection capacity[11].

Crude oil production allocation is the equilibrium point of technical policy and management [12] and the scientific of production allocation method will be directly related to the effect of oilfield development [13], Scholars at home and abroad have done a lot of work in the study of production allocation methods [14-18]. However, most of the previous studies only considered the influence of single factor on crude oil production allocation, and the influence of multiple factors such as pressure sensitivity effect, starting pressure gradient and fluid physical properties on production allocation is almost blank.

In this paper, on the basis of previous studies, considering the change of fluid physical properties after CO<sub>2</sub> injection, and considering the influence of fluid physical properties on the nonlinear seepage of low permeability reservoirs, a mathematical model of CO<sub>2</sub>

gravity flooding in low permeability reservoirs considering pressure sensitive effect is established. At the same time, the trial algorithm and iterative method are used to solve the model, and the corresponding chart is drawn to analyze the influence of pressure sensitivity coefficient, formation dip angle, injection-production well spacing and gas injection speed on the reasonable production allocation of the reservoir. According to the actual data of A reservoir, the production of water flooding to CO<sub>2</sub> flooding in the reservoir is optimized.

## 2. ESTABLISHMENT OF THE MODEL

In the process of CO<sub>2</sub> gravity flooding in actual reservoir, the formation pressure from injection well to production well is gradually reduced. When the minimum miscible pressure of CO<sub>2</sub> is between the bottom hole flow pressure of injection well and the bottom hole flow pressure of production well, the seepage of crude oil and CO<sub>2</sub> in the formation will be divided into CO<sub>2</sub> miscible zone and CO<sub>2</sub> immiscible zone, as shown in figure 1.

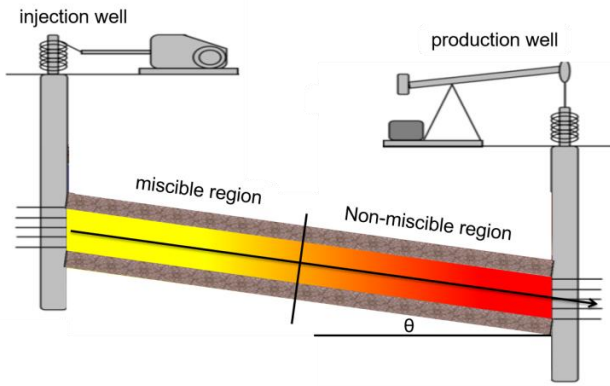


Fig. 1. CO<sub>2</sub> gravity drive seepage model

### 2.1 Assumed condition

In order to establish the seepage model of CO<sub>2</sub> gravity drive in low permeability reservoir, according to the actual characteristics of CO<sub>2</sub> gravity drive reservoir, the following assumptions are made.

(1) The reservoir is an inclined, homogeneous and equal-thick banded reservoir with length of  $X$ , width of  $B$ , thickness of  $h$  and dip angle of  $\theta$ .

(2) The reservoir is a low permeability reservoir, considering the influence of starting pressure gradient and pressure sensitivity effect.

(3) There are two phases of oil and gas in the reservoir, considering the influence of CO<sub>2</sub> on the viscosity and density of crude oil.

(4) The minimum miscible pressure is between the bottom hole flow pressure of gas injection well and

production well, and the fluid seepage area is composed of miscible zone and immiscible zone.

(5) There are two phases of oil and gas in the reservoir, considering the influence of CO<sub>2</sub> on the viscosity and density of crude oil.

### 2.2 CO<sub>2</sub> miscible zone model

When the formation pressure is greater than the minimum miscible pressure, CO<sub>2</sub> and crude oil form a miscible phase, and the fluid seepage in the miscible zone is a single-phase seepage. At the same time, considering the influence of starting pressure gradient and gravity, the Darcy formula is modified, and the flow rate through any section is:

$$q = \frac{KBh}{\mu_m} \left( \frac{dP}{dX} + \rho_m g \sin \theta - \lambda_m \right) \quad (1)$$

where  $q$  is the oil production of oil well, m<sup>3</sup>/d;  $K$  is formation permeability, mD;  $B$  is the stratum width, m;  $h$  is the thickness of stratum, m;  $\mu_m$  is the fluid viscosity in the miscible region, mPa·s;  $P$  is formation pressure, MPa;  $\rho_m$  is the fluid density in the miscible region, kg/m<sup>3</sup>;  $g$  is the gravity coefficient, N/kg;  $\theta$  is the formation dip angle, °;  $\lambda_m$  is the starting pressure gradient of the fluid in the miscible region, MPa/m.

Substitute the boundary conditions: when  $X=0$ ,  $P=P_{iwf}$ ; when  $X=X_m$ ,  $P=P_{mm}$ , and integral, get:

$$P_{mm} - P_{iwf} = \int_0^{X_m} \left( \frac{q\mu_m}{KBh} + \rho_m g \sin \theta - \lambda_m \right) dx \quad (2)$$

where  $P_{mm}$  is the minimum miscibility pressure, MPa;  $P_{iwf}$  is the bottom hole pressure of the gas injection well, MPa;  $X_m$  is the length of the miscibility zone, m.

The fluid density and viscosity in the miscible region can be calculated by the following formula:

$$\mu_m = \mu_g C + \mu_o (1 - C) \quad (3a)$$

$$\rho_m = \rho_g C + \rho_o (1 - C) \quad (3b)$$

where  $\mu_g$  is the viscosity of CO<sub>2</sub> gas, mPa·s;  $C$  is the concentration of CO<sub>2</sub>, decimal;  $\mu_o$  is crude oil viscosity, mPa·s;  $\rho_g$  is the density of CO<sub>2</sub>, kg/m<sup>3</sup>;  $\rho_o$  is crude oil density, kg/m<sup>3</sup>.

In the CO<sub>2</sub> miscible region, the concentration of CO<sub>2</sub> is different at different positions. The viscosity and density of the fluid in the miscible region are required. The concentration of CO<sub>2</sub> in the fluid needs to be obtained first. The distribution law can be characterized by the following formula [19]:

$$C(x,t) = \frac{1}{2} e^{\frac{vx}{2D}} \cdot e^{-\xi x} \times \left( \operatorname{erf} \frac{x - \sqrt{u^2 + 4\beta D} \cdot t}{2\sqrt{Dt}} \right. \\ \left. + \operatorname{erf} \frac{x + \sqrt{u^2 + 4\beta D} \cdot t}{2\sqrt{Dt}} \right) \quad (4)$$

where  $v$  is seepage velocity, m/s;  $\xi$  is the velocity coefficient of particle capture,  $m^{-1}$ ;  $D$  is the diffusion coefficient of  $CO_2$  in crude oil,  $m^2/s$ ;  $\beta$  is the adsorption velocity coefficient of particles on the rock surface

The permeability calculation formula considering the pressure-sensitive effect [20,21]:

$$K = K_0 e^{-M(P_1 - P)} \quad (5)$$

where  $K_0$  is original formation permeability, mD;  $M$  is the pressure-sensitive coefficient,  $MPa^{-1}$ ;  $P_1$  is original formation pressure, MPa.

The calculation formula of variable start-up pressure gradient considering pressure-sensitive effect [22]:

$$\lambda_m = a \left( \frac{K_0}{\mu_m} \right)^{-b} e^{bM(P_1 - P)} \quad (6)$$

where  $a$ ,  $b$  are positive real numbers.

Formula (1) ~ (6) is the mathematical model of the miscible phase of  $CO_2$  gravity flooding in low permeability reservoirs considering the pressure-sensitive effect.

### 2.3 $CO_2$ immiscible zone model

The area where the formation pressure is less than the minimum miscible pressure is called the  $CO_2$  immiscible zone, and the fluid seepage in this area is oil-gas two-phase seepage. Considering the influence of  $CO_2$  dissolution on the physical properties of crude oil, the starting pressure gradient of oil phase and the pressure sensitivity effect, the basic differential equation of one-dimensional seepage of  $CO_2$ -crude oil two-phase non-Darcy gravity flooding phase is as follows: get:

$$\frac{\partial}{\partial x} \left[ \frac{KK_{ro}}{\mu_{io}} \left( \frac{\partial p}{\partial x} + \rho_{io} g \sin \theta - \lambda_{io} \right) \right] = \varphi \frac{\partial S_o}{\partial t} \quad (7a)$$

$$\frac{\partial}{\partial x} \left[ \frac{KK_{rg}}{\mu_g B_g} \left( \frac{\partial p}{\partial x} + \rho_g g \sin \theta - \lambda_g \right) + \frac{R_s KK_{ro}}{\mu_{io} B_o} \left( \frac{\partial p}{\partial x} + \rho_{io} g \sin \theta - \lambda_{io} \right) \right] = \quad (7b)$$

$$\varphi \frac{\partial}{\partial t} \left( \frac{1 - S_o}{B_g} + \frac{S_o R_s}{B_o} \right)$$

where  $K_{ro}$  is the relative permeability of oil phase, decimal;  $\mu_{io}$  is the viscosity of oil phase in immiscible

region, mPa·s;  $\rho_{io}$  is the oil phase density in immiscible region,  $kg/m^3$ ;  $\lambda_{io}$  is the starting pressure gradient of oil phase in immiscible region, MPa/m;  $\varphi$  is porosity, decimal;  $S_o$  is oil saturation, decimal.  $K_{rg}$  is the relative permeability of gas phase, decimal;  $\lambda_g$  is the gas phase start-up pressure gradient in the immiscible region, MPa/m;  $B_g$  is the volume coefficient of  $CO_2$ ,  $m^3/m^3$ ;  $B_o$  is the volume coefficient of crude oil,  $m^3/m^3$ ;  $R_s$  is the solubility of  $CO_2$  in crude oil,  $m^3/m^3$ .

The flow through any section is:

$$q = KBh \left[ \frac{K_{rg}}{\mu_g} \left( \frac{\Delta P}{\Delta x} + \rho_g g \sin \theta - \lambda_g \right) + \right. \quad (8)$$

$$\left. \frac{K_{ro}}{\mu_{io}} \left( \frac{\Delta P}{\Delta x} + \rho_{io} g \sin \theta - \lambda_{io} \right) \right]$$

The pressure difference is:

$$\Delta P = \frac{\Delta x}{\frac{K_{rg}}{\mu_{ig}} + \frac{K_{ro}}{\mu_{io}}} \left[ \frac{K_{rg}}{\mu_{ig}} (\rho_{ig} g \sin \theta - \lambda_{ig}) \right. \quad (9)$$

$$\left. + \frac{K_{ro}}{\mu_{io}} (\rho_{io} g \sin \theta - \lambda_{io}) - \frac{q}{KBh} \right]$$

The relative permeability of oil and gas phase is a function of gas saturation, which can be obtained by relative permeability curve fitting:

$$K_{rg} = 0.06 \left( \frac{S_g}{1 - S_{or}} \right)^{2.39} \quad (10a)$$

$$K_{ro} = 1.23 \left( \frac{S_g}{1 - S_{or}} \right)^{3.353} \quad (10b)$$

where  $S_g$  is gas saturation, decimal;  $S_{or}$  is the residual oil saturation, decimal.

$CO_2$  is constantly dissolved in crude oil, and the physical properties of the fluid in the formation are constantly changing. The formula (11) can be used to correct the viscosity and density of the oil phase in the  $CO_2$  immiscible zone [23]:

$$\mu_{io} = \mu_o^{1 - Y_g} \times \mu_g^{Y_g} \quad (11a)$$

$$\rho_{io} = \rho_o^{1 - Y_g} \times \rho_g^{Y_g} \quad (11b)$$

where  $Y_g$  is the proportion of  $CO_2$  component in oil phase, decimal.

The formula (12) can be used to correct the proportion of  $CO_2$  component in oil phase [24]:

$$Y_g = \frac{1}{\alpha F_g / (5.618 F_o R_s) + 1} \quad (12)$$

where  $\alpha$  is a constant related to temperature and pressure, decimal;  $F_g$  is the ratio of the volume of  $CO_2$

under standard conditions to the volume under reservoir conditions,  $m^3/m^3$ ;  $F_o$  is the ratio of the volume of crude oil under reservoir temperature and 0.1MPa pressure to the volume under reservoir volume,  $m^3/m^3$ .

The starting pressure gradient of oil phase and gas phase considering pressure sensitivity effect in immiscible region:

$$\lambda_{i_o} = a \left( \frac{K}{\mu_{i_o}} \right)^{-b} e^{bM(P_i - P)} \quad (13a)$$

$$\lambda_g = a \left( \frac{K}{\mu_g} \right)^{-b} e^{bM(P_i - P)} \quad (13b)$$

Formula (7) ~ (13) is the mathematical model of immiscible part of CO<sub>2</sub> gravity flooding in low permeability reservoirs considering pressure-sensitive effect.

### 3. SOLUTION AND ANALYSIS OF THE MODEL

#### 3.1 CO<sub>2</sub> miscible zone solution method

Considering the pressure-sensitive effect, the formation permeability and starting pressure gradient of the fluid affecting the flow of CO<sub>2</sub> gravity drive vary with the change of pressure, and the pressure gradient at each point is not constant. Therefore, the fluid seepage in the miscible region considering the pressure-sensitive effect needs to be calculated in sections, and the seepage parameters (permeability, viscosity, density and starting pressure gradient) of each section need to be obtained in advance. However, permeability and start-up pressure gradient are functions of pressure, and pressure is an unknown number in calculation, so CO<sub>2</sub> gravity drive needs to be calculated by trial algorithm and iterative method. Because the pressure at both ends of the miscible region is known, the iterative calculation is performed with length increment. The steps are as follows:

(1) Taking the bottom hole flowing pressure  $P_{i_{wf}}$  of the gas injection well as the starting point, an appropriate pressure drop  $\Delta P$  is taken as the calculated pressure interval.

(2) Assuming that a corresponding  $\Delta P$  corresponds to the corresponding  $\Delta X$ , according to Eq. (4) to determine the CO<sub>2</sub> concentration distribution in this section.

(3) Calculate the formation pressure  $P_i$  and CO<sub>2</sub> mole fraction  $C_i$  at the right end of the section, and determine the seepage parameters (formation permeability, fluid viscosity, fluid density and starting pressure gradient,

etc.) under the  $P_i$  and  $C_i$  according to equation (3), (5) and(6).

(4) According to the formula (1), the length  $\Delta X_j$  corresponding to  $\Delta P$  is calculated.

(5) Comparing the  $\Delta X_j$  calculated in step (4) with the  $\Delta X$  assumed in step (2), both of which exceed the allowable error range, the new  $\Delta X$  is used as the assumed value, and the calculation from (2) to (4) is repeated, so that the error between the calculated  $\Delta X_j$  and  $\Delta X$  is within the allowable error range.

(6) Calculate the displacement distance  $X_i$  and formation pressure  $P_i$  corresponding to the right end of this section.

$$X_I = \sum_{j=1}^I X_j \quad (14)$$

$$P_i = P_{i_{wf}} - I \Delta P \quad (15)$$

(7) Taking the pressure at  $X_i$  as the starting point, repeat steps (2) to (6), calculate the length displacement distance  $X_{i+1}$  and formation pressure  $P_{i+1}$  in the next step, until the formation pressure is equal to or less than the minimum miscibility pressure, and obtain the length of the miscibility zone  $X_{mm}$ .

#### 3.2 CO<sub>2</sub> immiscible zone model

The relative permeability of oil phase and CO<sub>2</sub> gas phase in CO<sub>2</sub> immiscible zone is a function of gas saturation, and the formation permeability is a function of pressure. Therefore, in order to solve the CO<sub>2</sub> immiscible flooding model, the saturation distribution and pressure distribution in the area must be solved first. According to the Buckley-Leverett displacement theory, the equation of motion of the front edge of equal saturation is:

$$X - X_0 = \frac{1}{\phi A} \frac{df_g(S_g)}{dS_g} Q(t) \quad (16)$$

where  $Q(t)$  is the total flow through the seepage section,  $m^3$ .

Because the injection-production well spacing is known, the length of the miscible zone is solved according to the seepage of the CO<sub>2</sub> miscible zone, and the length of the immiscible zone is:

$$X_{im} = \frac{L}{\cos \theta} - X_{mm} \quad (17)$$

where  $X_{im}$  is the length of immiscible region, m;  $L$  is the injection-production well spacing, m.

The immiscible region is divided into  $n$  equal parts. Substituting  $X=X_{i+1}$ ,  $X=X_i$  into Eq. (16) and subtracting, we get:

$$\Delta X_1 = \frac{Q(t)}{\varphi A} \left\{ \frac{df_g[S_{g(I+1)}]}{dS_{g(I+1)}} - \frac{df_g[S_{g(I)}]}{dS_{g(I)}} \right\} \quad (18)$$

Because the length of the two ends of the immiscible zone is known, the iterative calculation is carried out with the pressure increment pair (9). The steps are as follows:

(1) Select the appropriate displacement length  $\Delta X$  with the minimum miscible pressure  $X_{mm}$  pressure  $P_{mm}$  as the starting point.

(2) Estimate the  $\Delta P$  corresponding to a corresponding displacement length  $\Delta X$ .

(3) According to formula (10) and (16), the relative permeability of oil phase and  $CO_2$  phase in this section is calculated. Combined with formula (5), formula (11) and (13), the formation permeability, fluid density, fluid viscosity and starting pressure gradient of oil phase and  $CO_2$  phase in this section are calculated.

(4) The pressure change  $\Delta P_j$  of this section is calculated according to Eq. (9)

(5) Comparing the estimated  $\Delta P$  and  $\Delta P_j$ , if the error between the two is within the allowable error range, the calculated value is used as a new estimate, and steps (2) to (4) are repeated until the error between the two is within the allowable range.

(6) Calculate the displacement distance  $X_1$  and pressure  $P_1$  of the right end of the segment.

$$X - X_0 = \frac{1}{\varphi A} \frac{df_g(S_g)}{dS_g} Q(t) \quad (19)$$

$$X - X_0 = \frac{1}{\varphi A} \frac{df_g(S_g)}{dS_g} Q(t) \quad (20)$$

(7) Repeat steps (2) to (6) with the pressure  $P_1$  at  $X_1$  as the starting point. Calculate the length of the next section  $X_{i+1}$  and the pressure  $P_{i+1}$  until  $X_i$  is equal to or greater than  $L/\cos\theta$ , and output  $P_{wf}$ .

### 3.3 Parameter sensitivity analysis

#### 3.3.1 Pressure-sensitive coefficient

Keeping the injection-production well spacing, gas injection volume, formation dip angle and other parameters unchanged, only the pressure sensitivity coefficient is changed, and the reasonable production allocation of different bottom hole flow pressure is calculated when the pressure sensitivity coefficient is different, and the map is drawn, as shown in Figure 2. From the diagram, it can be seen that with the increase of pressure sensitivity coefficient, the bottom hole flowing pressure-reasonable production allocation curve

moves downward; at the same time, it can be found that the greater the bottom hole flow pressure, the smaller the influence of the pressure sensitivity coefficient on the reasonable production allocation. This is because the pressure sensitivity coefficient represents the degree of damage to the reservoir caused by the change of formation pressure. That is to say, when the formation pressure is the same, the larger the pressure sensitivity coefficient is, the greater the resistance of the fluid seepage in the reservoir is, which leads to the smaller the reasonable production of the reservoir. At the same time, it also shows that increasing the bottom hole flow pressure can effectively reduce the damage of the pressure effect on the reservoir. When the pressure sensitivity coefficient is 0, that is, without considering the influence of pressure sensitivity effect, the reasonable production allocation of the reservoir is relatively high.

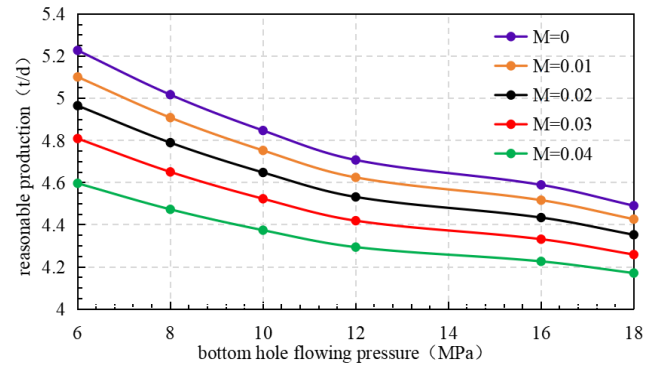


Fig. 2. The influence of pressure-sensitive coefficient on reasonable production allocation

#### 3.3.2 Stratigraphic dip

Keeping the parameters such as pressure sensitivity coefficient, injection-production well spacing and gas injection velocity unchanged, only changing the size of formation dip angle, the reasonable production allocation of different bottom hole flow pressure under different formation dip angle conditions is calculated, and the chart is drawn, as shown in figure 3. It can be seen from the figure that as the formation dip angle increases, the bottom hole flowing pressure-reasonable production curve moves upward, indicating that under the same bottom hole flowing pressure conditions, the reasonable production of the reservoir increases with the increase of the formation dip angle. This is because the greater the dip angle of the formation, the greater the gravitational potential energy of the fluid, and for gravity-driven reservoirs, the gravitational potential energy can provide power for fluid seepage, that is, when under the same displacement pressure difference, the greater the dip angle of the formation, the easier the fluid flows, and the greater the seepage velocity,



resulting in a reasonable allocation of reservoir production becomes larger.

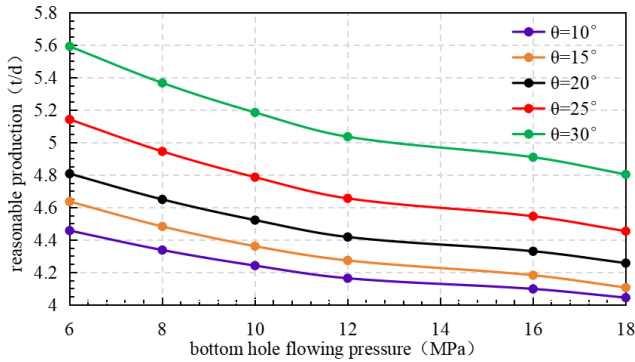


Fig. 3. The influence of formation dip angle on reasonable production allocation

### 3.3.3 Injection-production well spacing

Keep the parameters such as pressure sensitivity coefficient, formation dip angle and gas injection velocity unchanged, only change the size of injection-production well spacing, calculate the reasonable production allocation of different bottom hole flowing pressure under different injection-production well spacing conditions, and draw the map, as shown in Fig.4. From the diagram, it can be seen that with the increase of injection-production well spacing, the bottom hole flowing pressure-reasonable production allocation curve moves downward, indicating that under the same bottom hole flowing pressure, the reasonable production allocation of the reservoir decreases with the increase of injection-production well spacing. This is because the larger the injection-production well spacing, the greater the energy consumed by the fluid in the formation seepage, resulting in the smaller the reasonable allocation of the reservoir.

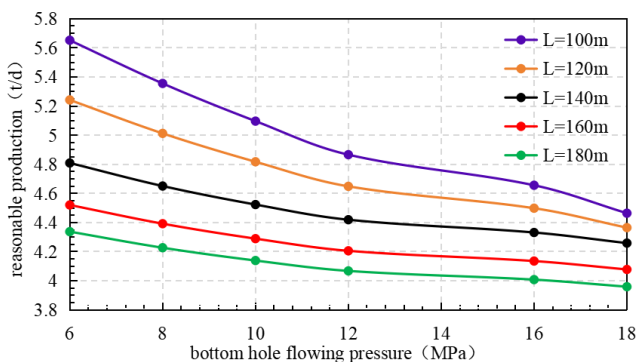


Fig. 4. The influence of injection-production well spacing on reasonable production allocation

### 3.3.4 Gas injection rate

Keeping the parameters such as pressure sensitivity coefficient, formation dip angle and injection-production well spacing unchanged, only changing the size of gas injection speed, the reasonable production allocation of different bottom hole flow pressure under different gas injection speed conditions is calculated, and the chart is drawn, as shown in figure 5. From the diagram, it can be seen that with the increase of gas injection speed, the bottom hole flow pressure-reasonable production allocation curve moves upward, indicating that under the same bottom hole flow pressure, the reasonable production allocation of the reservoir increases with the increase of gas injection speed, and the increase of reasonable production allocation decreases with the increase of gas injection speed.

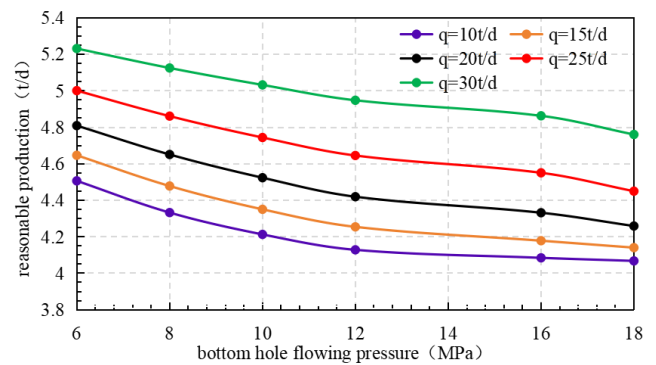


Fig. 5. The influence of gas injection rate on reasonable production allocation

## 4. APPLICATION

Taking A oilfield as an example, the reasonable production allocation after water flooding to CO<sub>2</sub> flooding is calculated by using the established model. The formation dip angle of this block is about 20°, the buried depth is 2500m, the porosity is 13.8%, the permeability is 3.4mD, the temperature is 85°C, the original formation pressure is 24.2MPa, the current pressure is 14.7MPa, and the well spacing is 140m. Through swelling, MMP, long core displacement and other experiments, under the original temperature and pressure conditions, the viscosity of crude oil is 2.752 mPa·s, and the viscosity reduction of crude oil is 66.6% after CO<sub>2</sub> injection. The minimum miscibility pressure of CO<sub>2</sub> and crude oil is 25MPa, and the pressure sensitivity coefficient is 0.03. The volume of CO<sub>2</sub> in the current reservoir is 2.68m<sup>3</sup>/d.

Table 1 Block statistics of increasing production multiples from water flooding to CO<sub>2</sub> flooding

Reservoir name	porosity/ (%)	permeability/ (mD)	crude oil density/ (g • cm <sup>-3</sup> )	crude oil viscosity/ (mPa • s)	Water drive production/ (m <sup>3</sup> /d)	CO <sub>2</sub> Flooding Production/ (m <sup>3</sup> /d)	production increase multiple/ (decimal)
Weyburn	12	15	0.887	4.700	2782.04	4479.00	1.61
Dollaride Devonial	17	9	0.830	0.400	119.41	192.00	1.61
Wertz tensleep	11	15	0.850	1.300	795.13	1701.00	2.14
Means San andres	9	20	0.880	6.000	1589.80	2941.00	1.85
North Cross	13	44	0.850	1.500	222.53	369.00	1.66
Slaughter Estate	12	8	0.870	2.000	33.38	66.10	1.98
Sinopec East China Oil	14	23	0.883	12.830	47.71	76.80	1.61
Pubei Block of Daqing	17.8	110	0.803	0.400	422.30	565.00	1.34
zhongyuan oil fields	27.2	245	0.748	2.020	4.76	14.60	3.07
Block Shu101 of Daqing	10	1	0.787	3.600	32.92	49.70	1.51
Hei 59 block of Jilin	10	5	0.769	1.970	50.07	76.60	1.53
Hei 79 block of Jilin	18	20	0.855	2.000	64.38	92.10	1.43

The reservoir engineering method, the current production system of the reservoir and the method of increasing production multiple are used to reasonably allocate the production in the work area. At the same time, tNavigator software is used to predict. The results are shown in Table 2. According to the method in this paper, the reasonable production allocation of the work area is determined to be 425 t / d, and the predicted recovery rate is high, up to 44.2 %, which indicates that the calculation method established in this paper can be well applied to the actual production of the oilfield.

Table 2 Analysis of reasonable production allocation

method	rationing production/(t·d <sup>1</sup> )	recovery ratio/(%)
Method of this article	425	44.2
The current production system	315	37.1
production increase multiple	450	40.6

## 5. CONCLUSION

(1) Based on the interaction between CO<sub>2</sub> and crude oil, combined with the complex seepage environment of low permeability reservoirs, a mathematical model of CO<sub>2</sub> gravity flooding considering the effect of pressure sensitivity and starting pressure gradient is established.

(2) Python programming software is used to solve the mathematical model, and different parameters are set to analyze the influence of four parameters, pressure sensitivity coefficient, formation dip angle, injection production well spacing and gas injection speed, on the reasonable production allocation of the reservoir. The larger the formation dip angle and gas injection speed, the larger the reasonable production allocation. The larger the pressure sensitivity coefficient and the injection-production well spacing, the smaller the reasonable production allocation.

(3) According to the actual parameters of A oilfield, the method of this paper, the current production system of the reservoir and the method of increasing production multiples are used to allocate the production in the work area. At the same time, tNavigator software is used to predict the recovery rate. The results show that the production system of 425t/d is determined according to the method of this paper, and the recovery rate of the reservoir is high, up to 44.2 %.

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## DECLARATION OF INTEREST STATEMENT

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper. All authors read and approved the final manuscript.

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